

$$\frac{dA_Z}{dt} = G_Z - C_A - C_Z$$

$$\frac{dA_E}{dt} = C_A - C_E + G_E \quad \text{etc.}$$

Zonal kinetic energy

$$\frac{\partial[u]}{\partial t} = [v] \left(f - \frac{\partial[u]}{\partial y} \right) + G + [F_x]$$

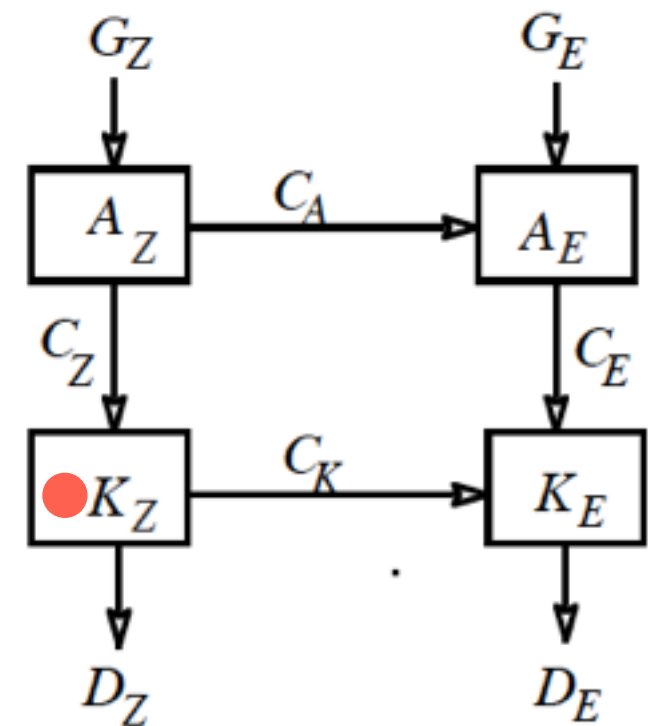
$$\frac{\partial \bar{K}_Z}{\partial t} = \underbrace{\frac{1}{g} \int_0^{p_0} f[\bar{u}][\bar{v}] dp}_{C_Z} + \underbrace{\frac{1}{g} \int_0^{p_0} [\bar{u}] G dp}_{-C_K} + \underbrace{\frac{1}{g} \int_0^{p_0} [\bar{u}][\bar{F}_x] dp}_{D_Z}$$

cross-isobar flow

eddy fluxes

friction

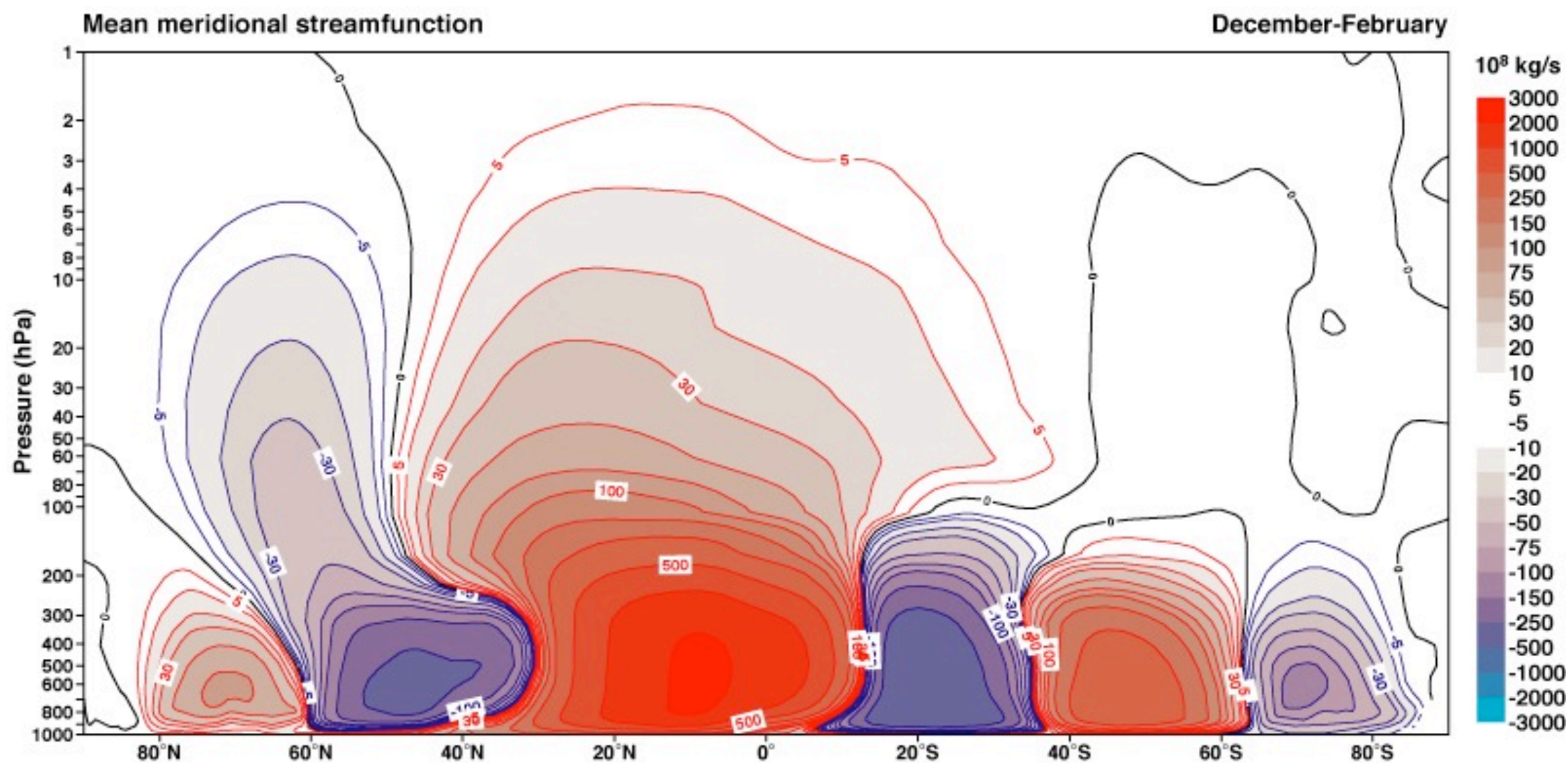
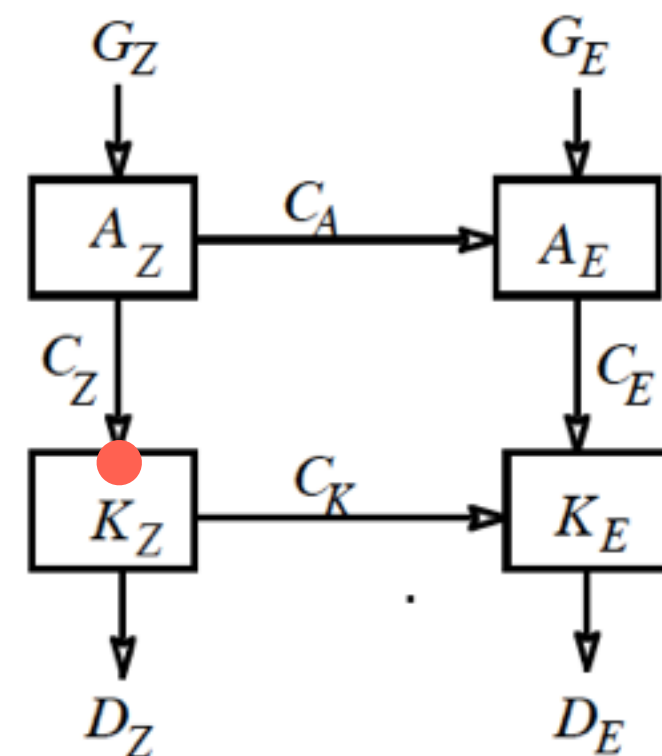
$$-[v] \frac{\partial[\Phi]}{\partial y}$$



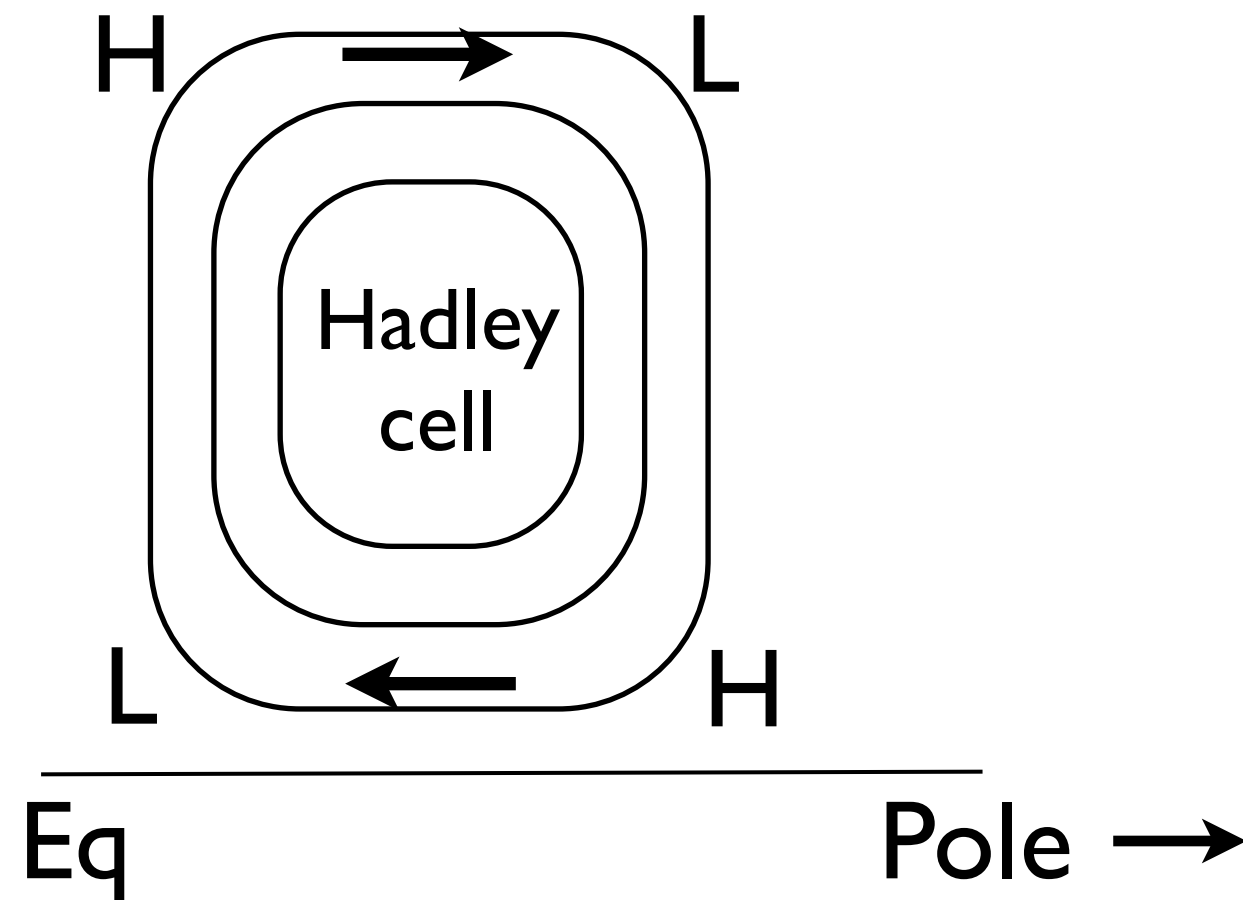
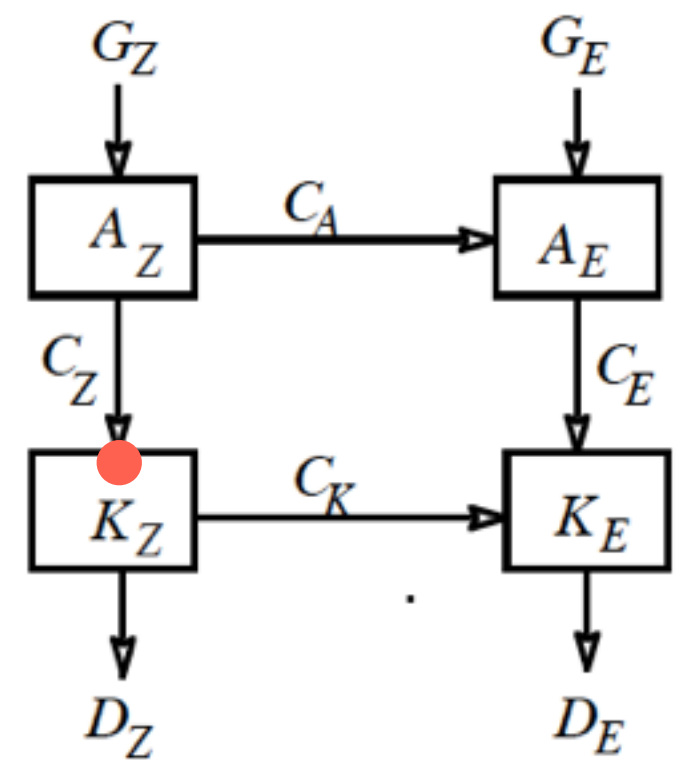
Note that in this section overbars denote global averages.

$$\frac{1}{g} \int_0^{p_0} f[u][v] dp$$

$$-[v] \frac{\partial [\Phi]}{\partial y}$$

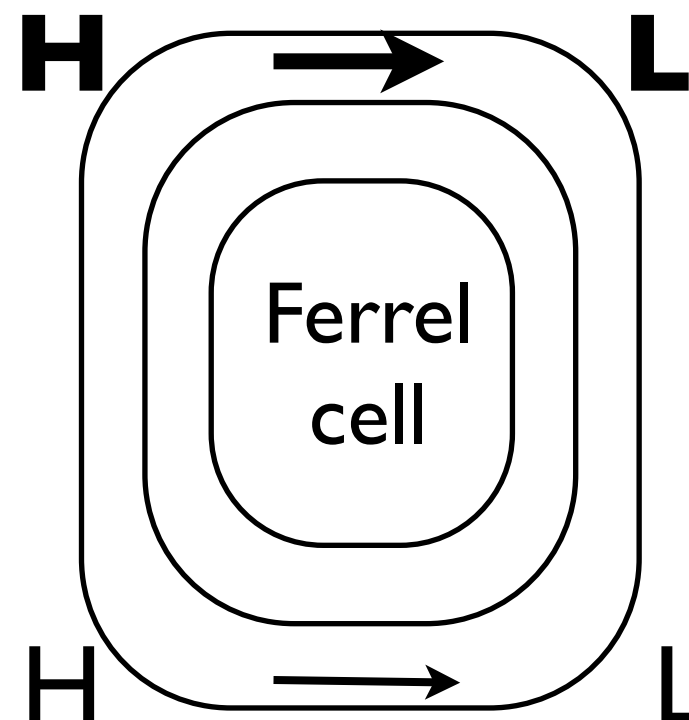
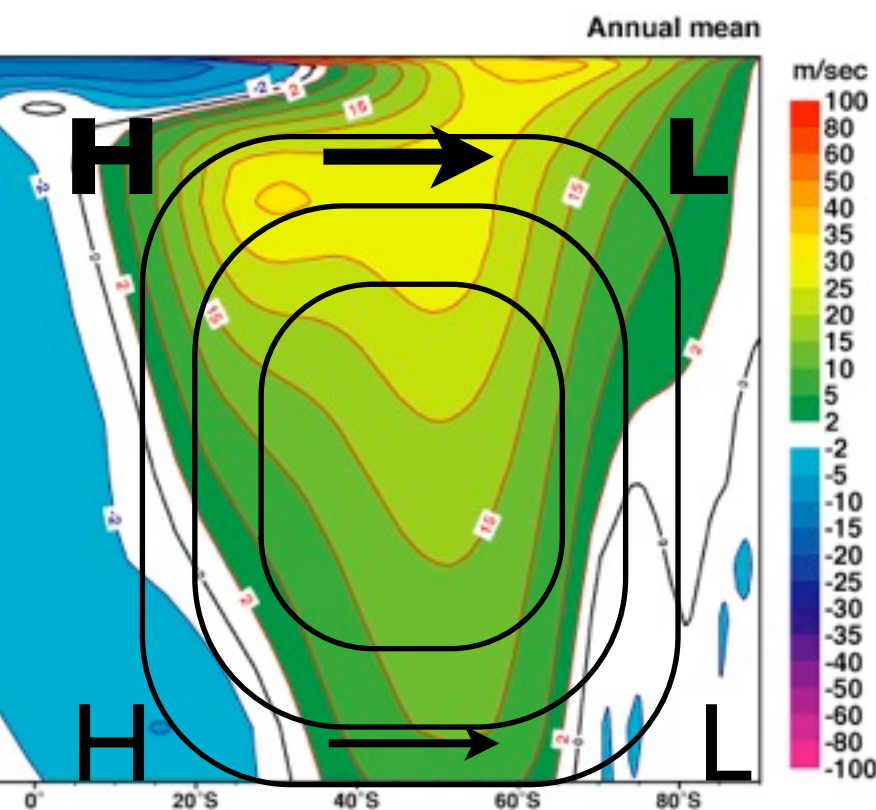
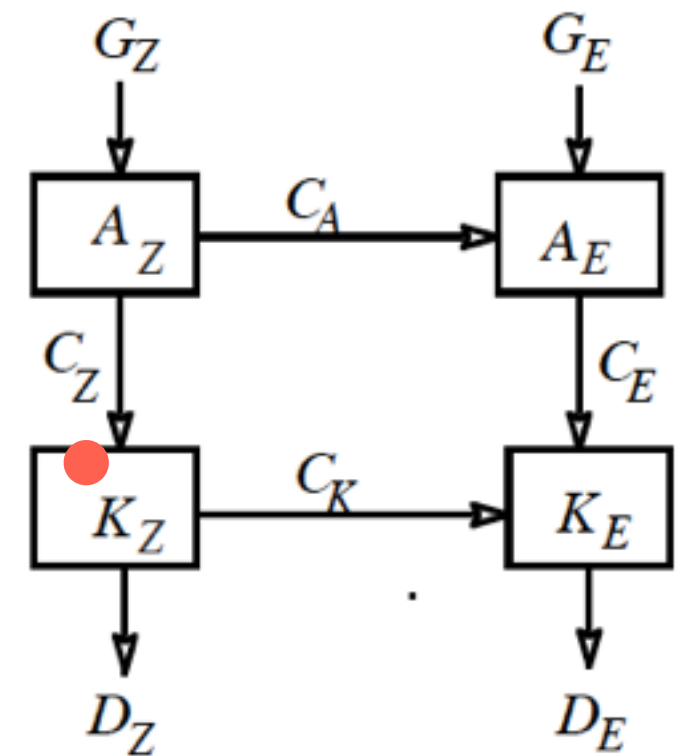


$$C_Z = \frac{1}{g} \int_0^{p_0} f[u][v] dp - [v] \frac{\partial[\Phi]}{\partial y}$$



Hadley Cell A_Z to K_Z i.e., thermally direct

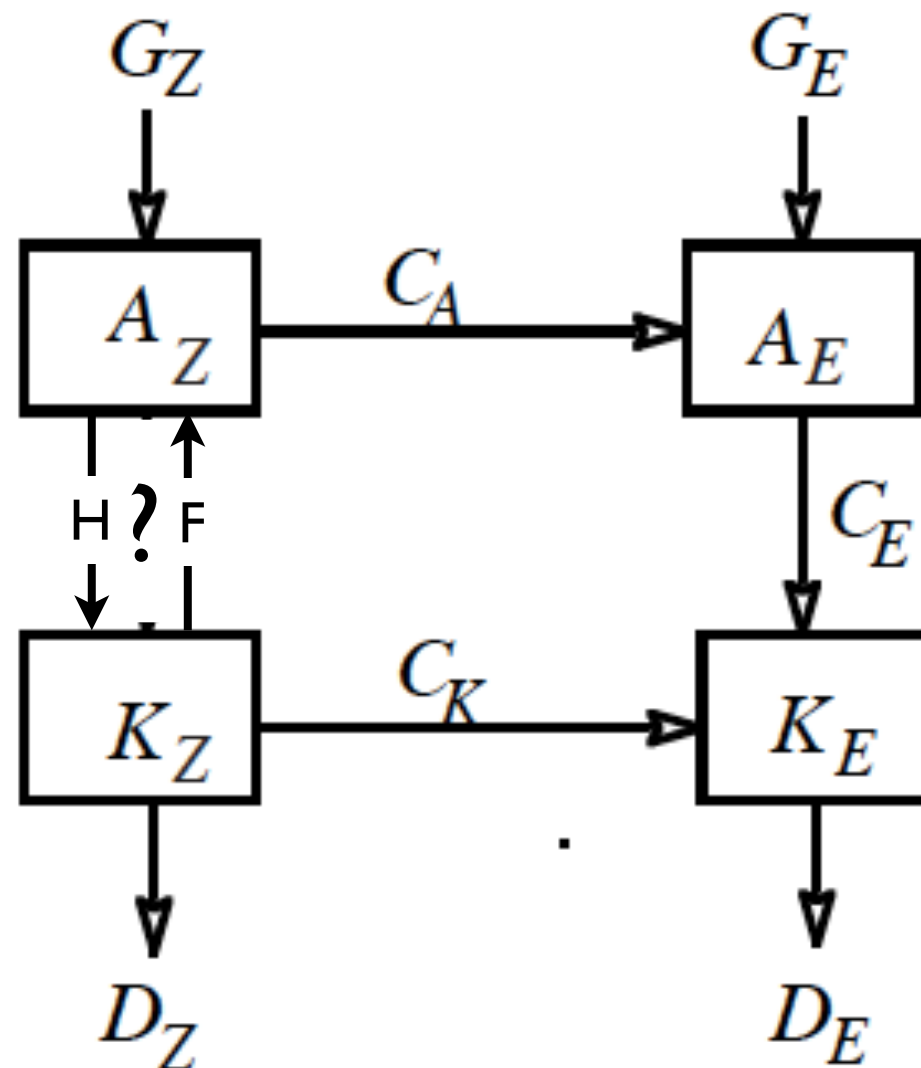
$$C_Z = \frac{1}{g} \int_0^{p_0} f[u][v] dp - [v] \frac{\partial [\Phi]}{\partial y}$$



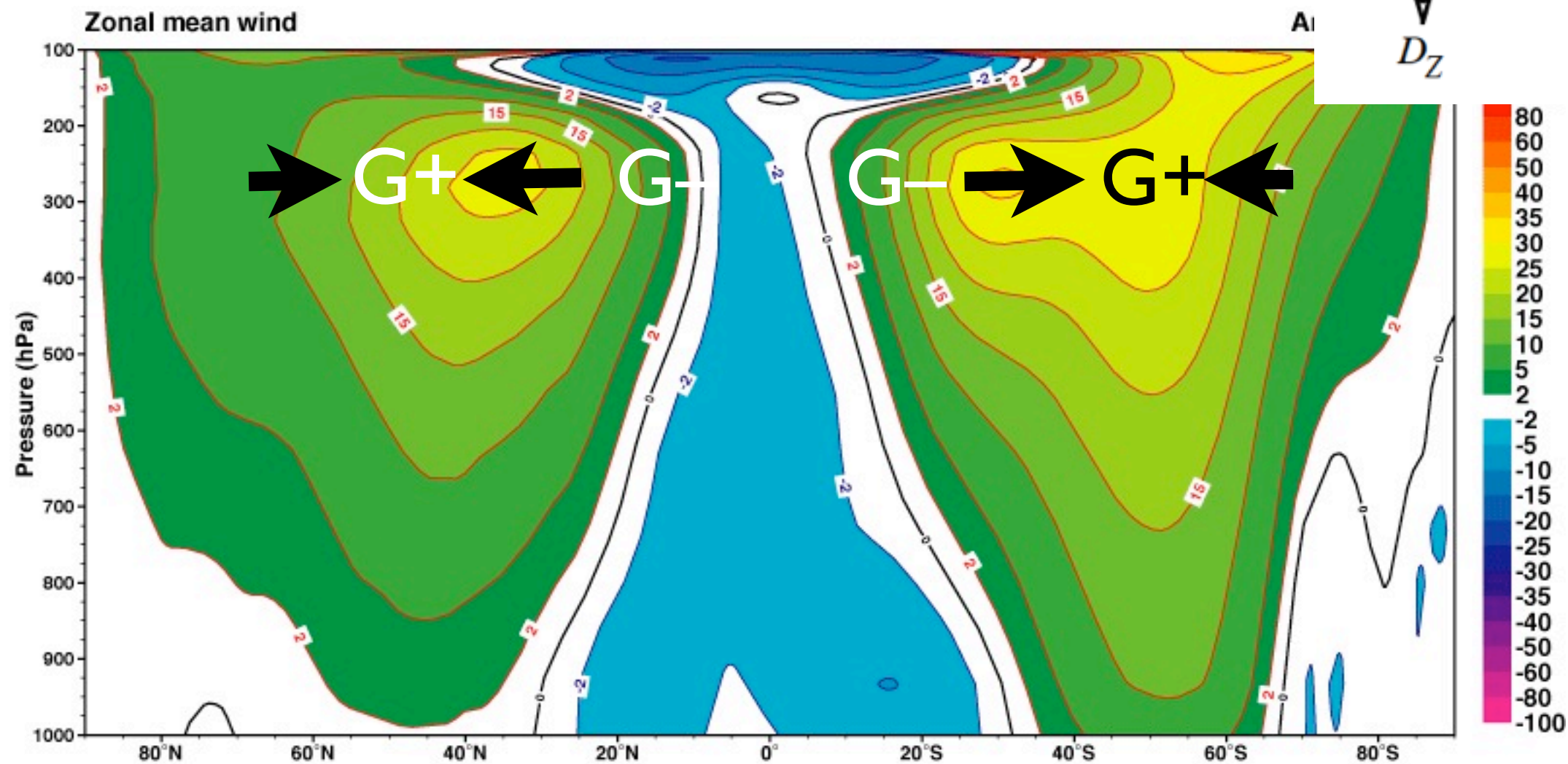
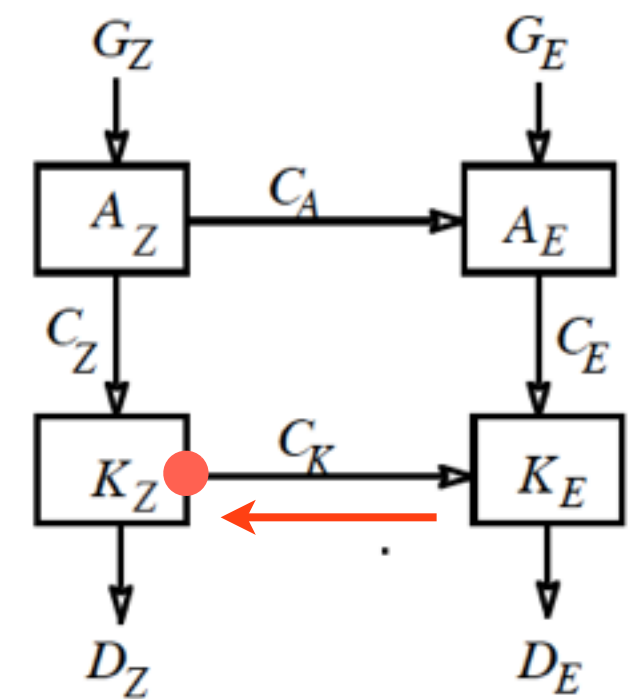
← Eq Pole →

Ferrell Cell K_Z to A_Z ; i.e., thermally indirect

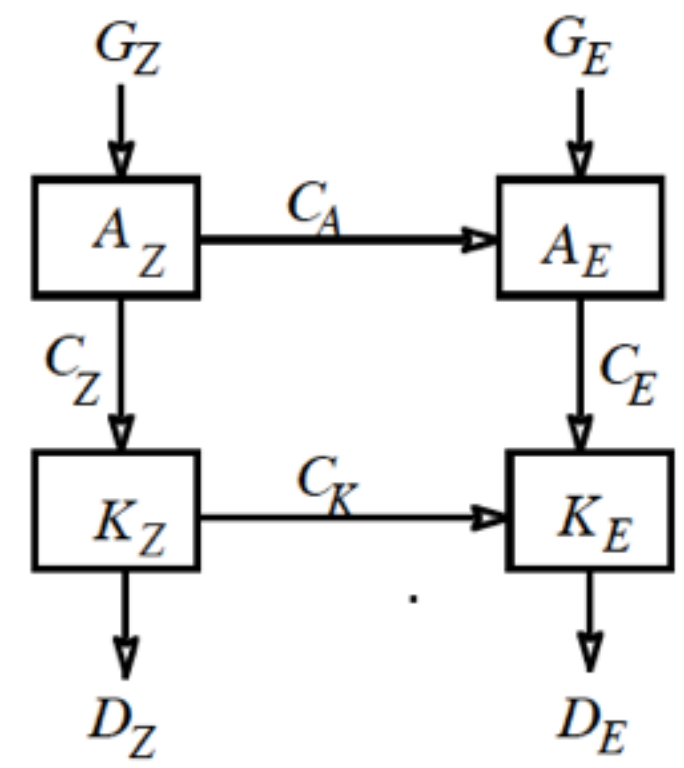
The conversions in the Hadley and Ferrell cells are nearly equal and opposite, so in the global-mean C_Z is small and even of uncertain sign.



$$-C_K = +\frac{1}{g} \int_0^{p_0} [\overline{u}] G dp$$

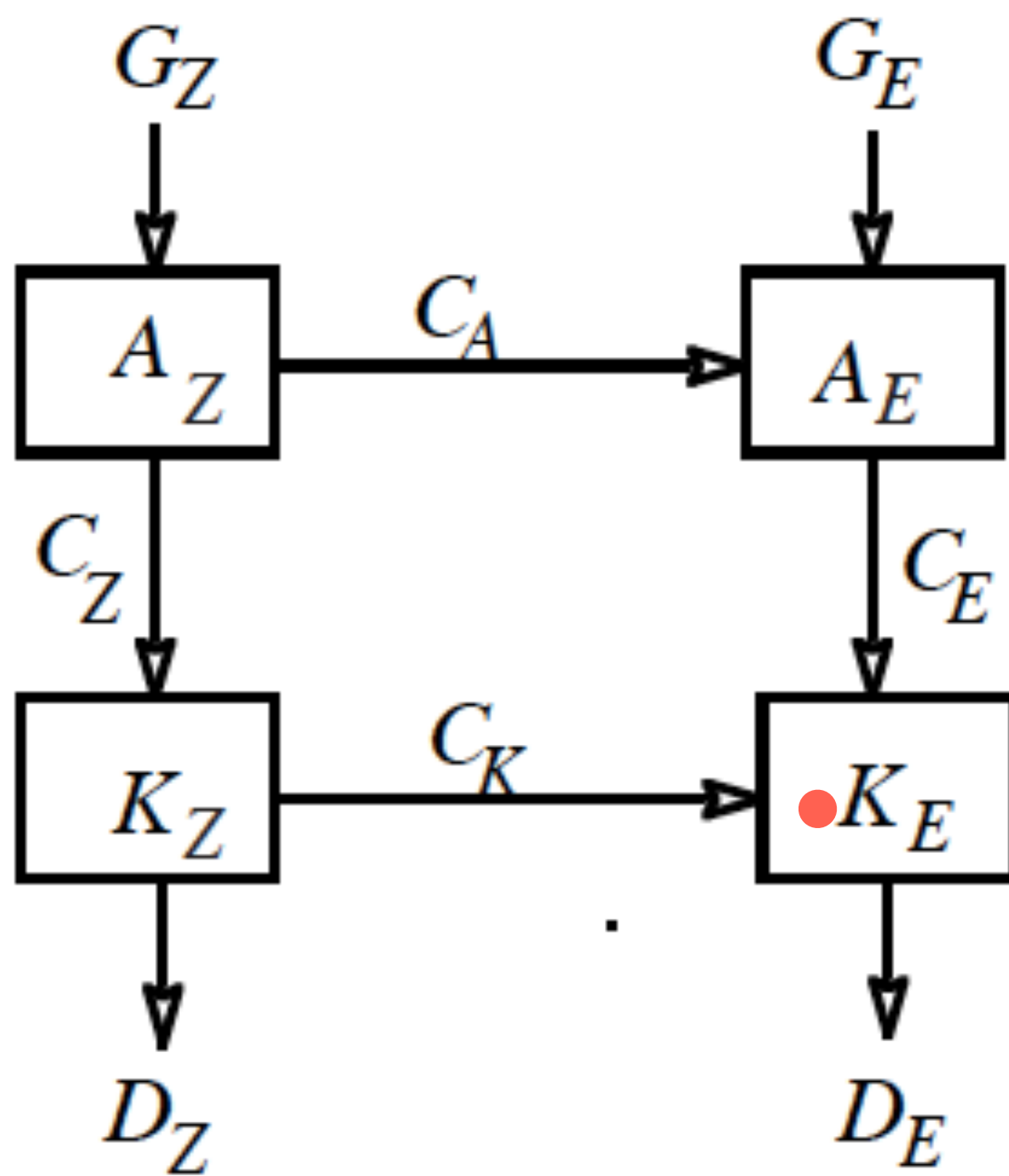


$G+$ where u is more positive so $-C_K > 0$



$$D_Z = - \frac{1}{g} \int_0^{p_0} \overline{[u][F_x]} dp$$

Frictional drag always yields positive D_Z



Eddy kinetic energy

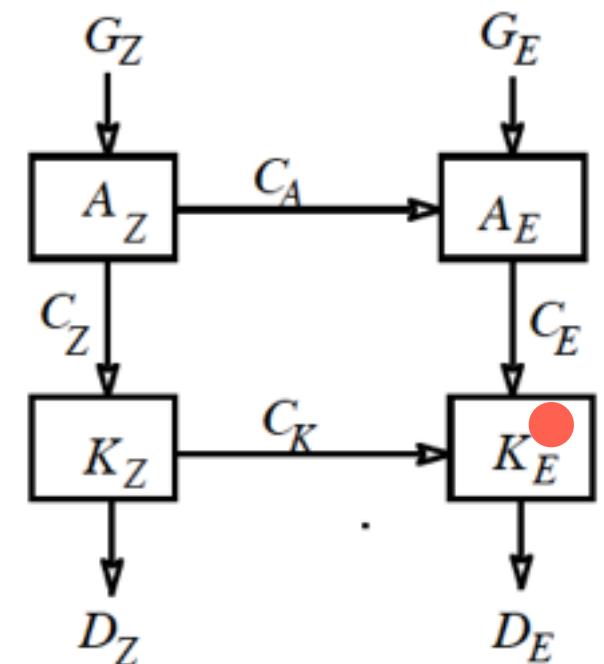
$$\frac{\partial \overline{K_E}}{\partial t} = \underbrace{-\frac{1}{g} \int_0^{p_0} \overline{[u^* v^*]} \frac{\partial [\overline{u}]}{\partial y} dp}_{C_K} - \underbrace{\frac{1}{g} \int_0^{p_0} \overline{\left[u^* \frac{\partial \Phi^*}{\partial x} + v^* \frac{\partial \Phi^*}{\partial y} \right]} dp}_{C_E} - \underbrace{\frac{1}{g} \int_0^{p_0} \overline{[u^* F_x^* + v^* F_y^*]} dp}_{D_E}$$

downgradient
momentum flux

cross-isobar flow

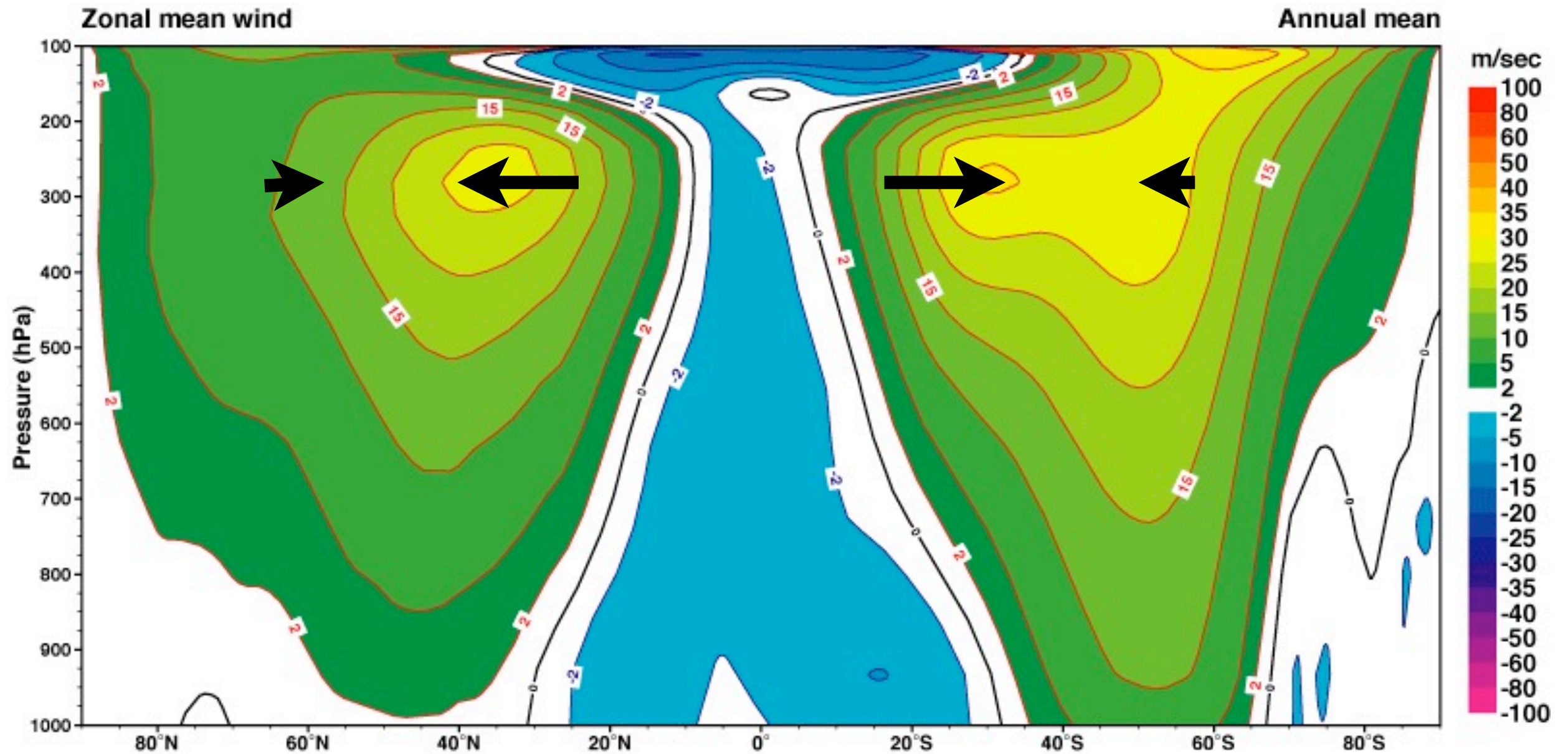
frictional drag

See Appendix 5 for a derivation.

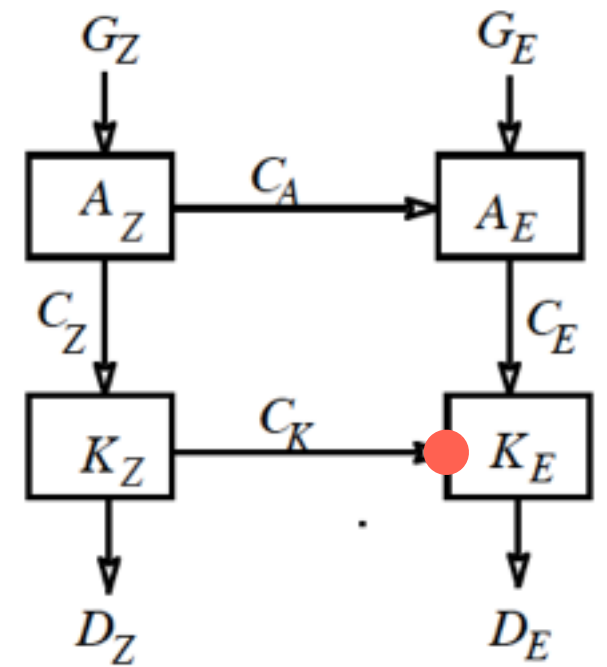


Note that the flux is primarily countergradient; i.e., toward higher u

u

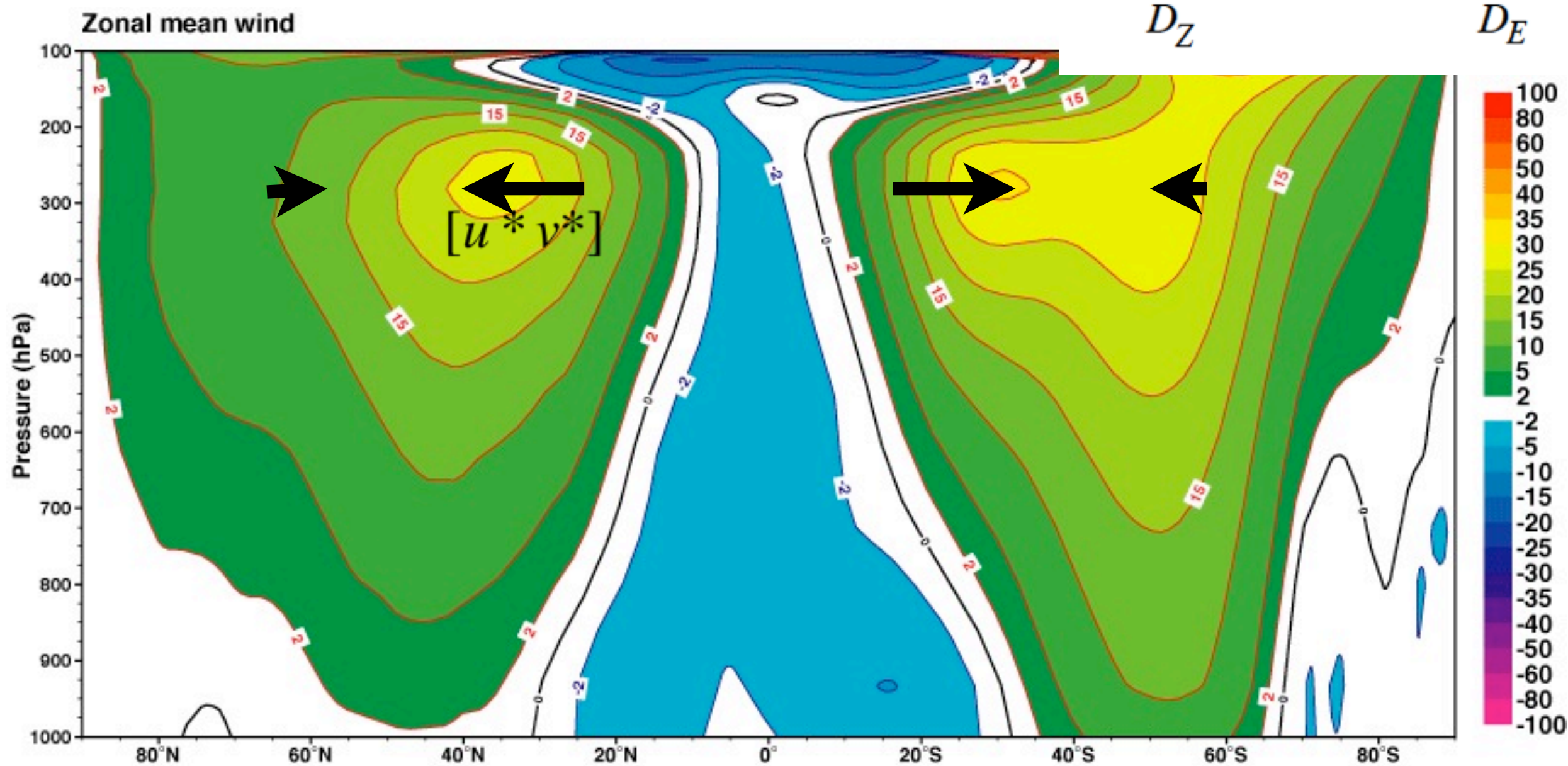
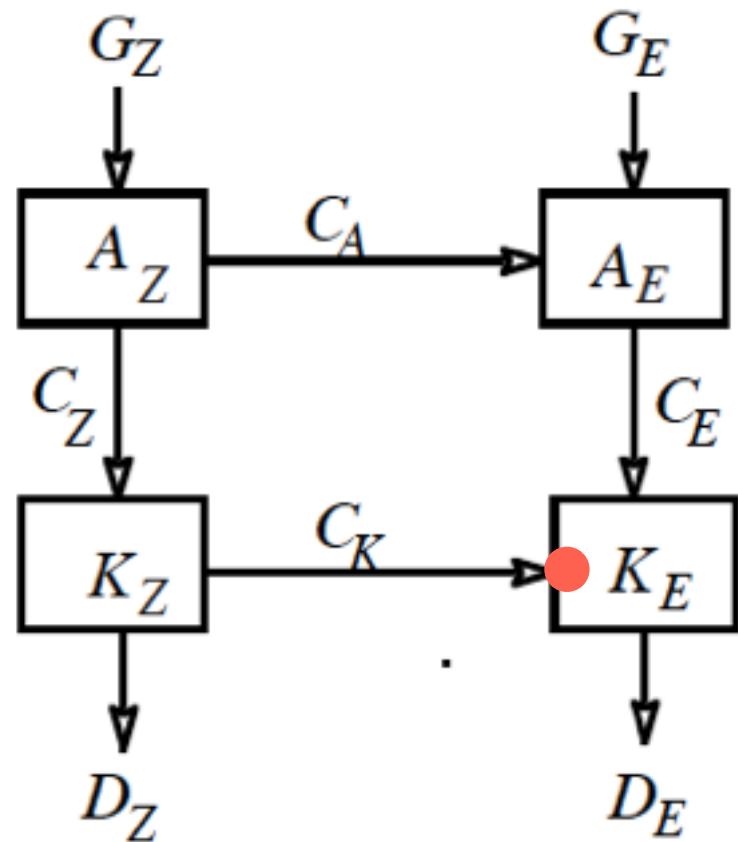


$$-\frac{1}{g} \int_0^{p_0} \overline{[u^* v^*]} \frac{\partial [u]}{\partial y} dp < 0$$



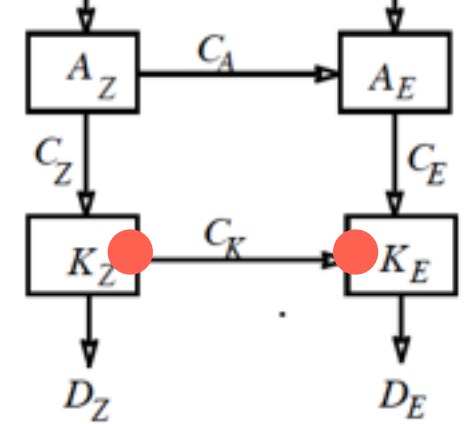
But the notion that mixing should be down-gradient doesn't really apply to zonal momentum, which doesn't behave as a passive tracer.

$$= -\frac{1}{g} \int_0^{p_0} \overline{[u^* v^*]} \frac{\partial [u]}{\partial y} dp$$



u

Note that



$$C_K = -\frac{1}{g} \int_0^{p_0} \overline{[u]G} dp = -\frac{1}{g} \int_0^{p_0} \overline{[u^* v^*] \frac{\partial [u]}{\partial y}} dp$$

Verify this identity substituting $G = -\frac{\partial}{\partial y} [u^* v^*]$

and noting that $\int_{pole}^{pole} \frac{\partial}{\partial y} [u] [u^* v^*] dy = 0$

It's only in the global average that the two expressions for C_K are identical.

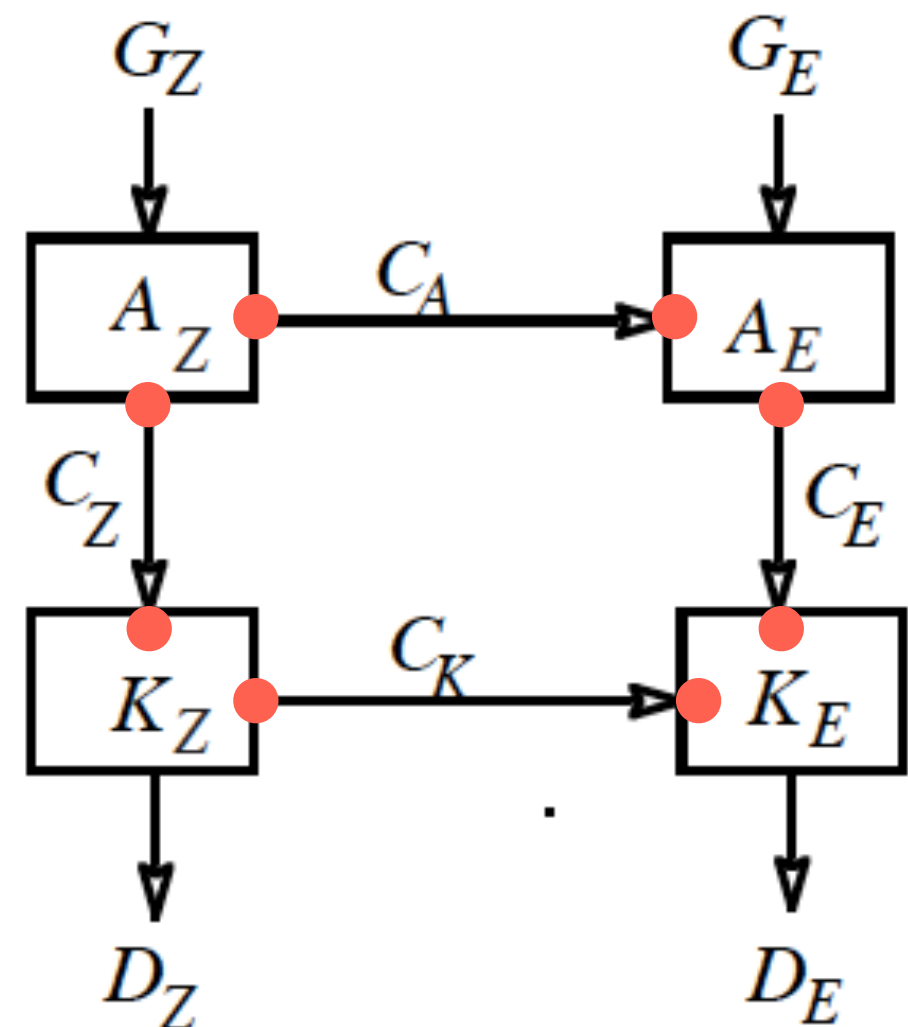


Joni Mitchell

In my song “*Clouds*”, I stressed that things often appear different when viewed from differing perspectives. Is that also true of the conversions in the Lorenz KE cycle?



That's right!



We can look at them from both sides now.



In the song, the punch line is
*“It’s clouds’ illusions I recall
I really don’t know clouds at all.”*



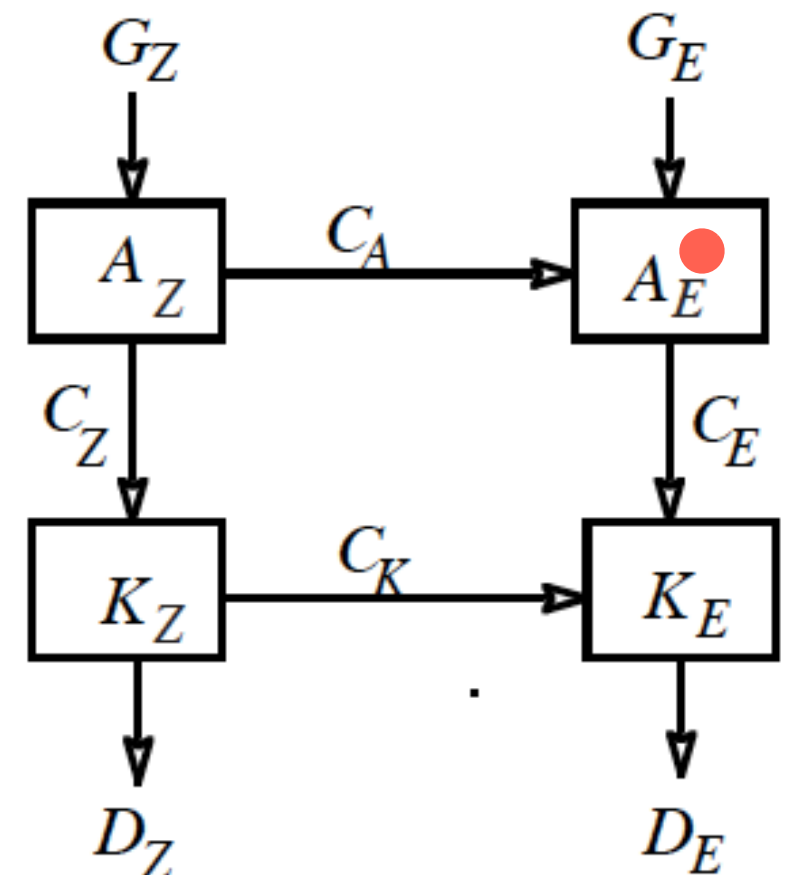
There are days when I wonder
about that too.

But compared to clouds
the Lorenz KE cycle is simple.

For the eddy available potential energy, we have

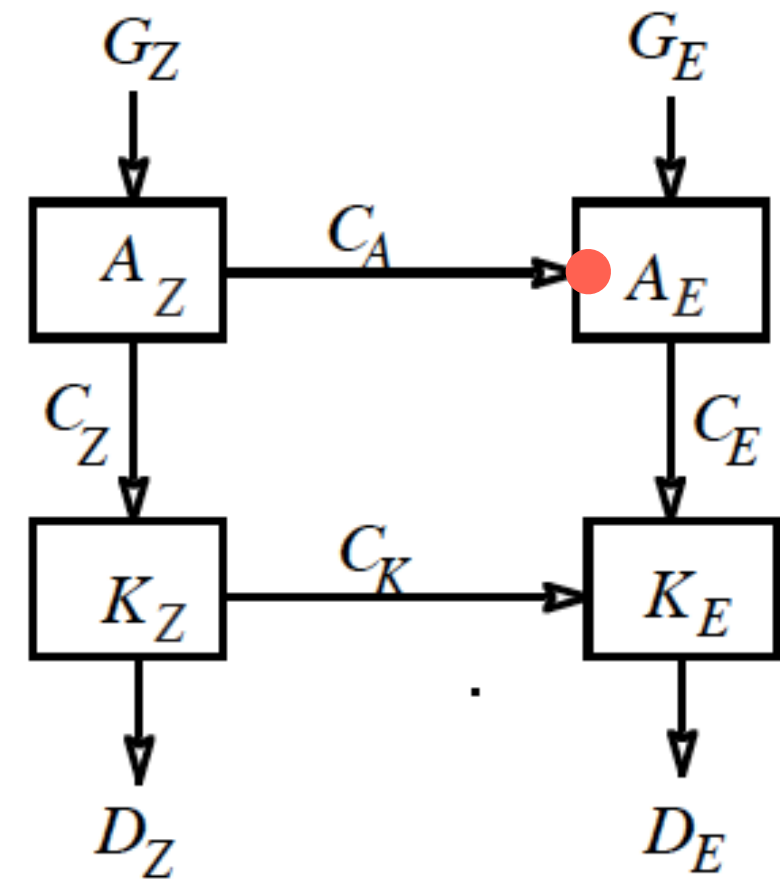
$$\frac{\partial A_E}{\partial t} = -\frac{1}{g} \int_0^{p_0} \overline{\left[\frac{v^* \alpha^*}{\sigma} \right]} \frac{\partial \alpha}{\partial y} dp + \frac{1}{g} \int_0^{p_0} \overline{[\omega^* \alpha^*]} dp + \frac{1}{g} \int_0^{p_0} \overline{\left[\frac{Q^* \alpha^*}{\sigma} \right]} dp$$

You should recognize the terms here.

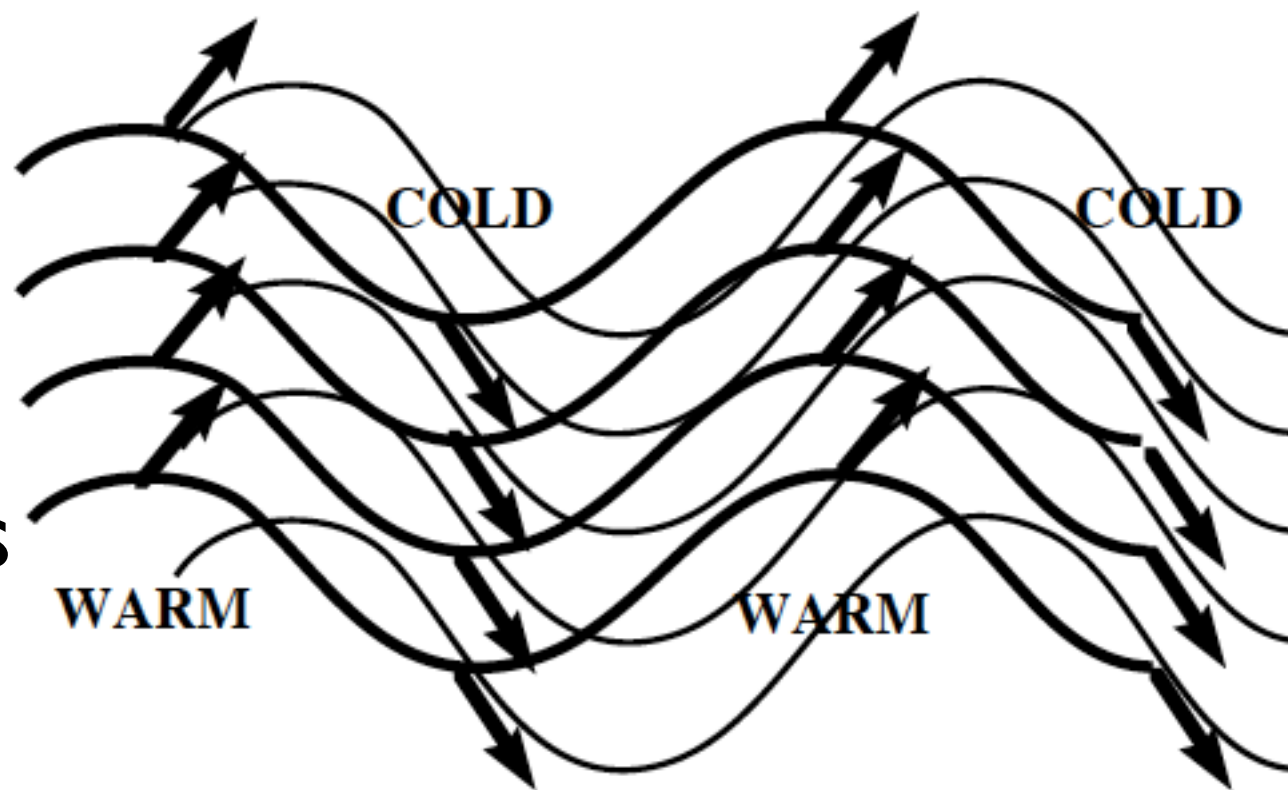


$$: -\frac{1}{g} \int_0^{p_0} \frac{[v^* \alpha^*]}{\sigma} \frac{\partial \alpha}{\partial y} dp.$$

the downgradient heat flux term



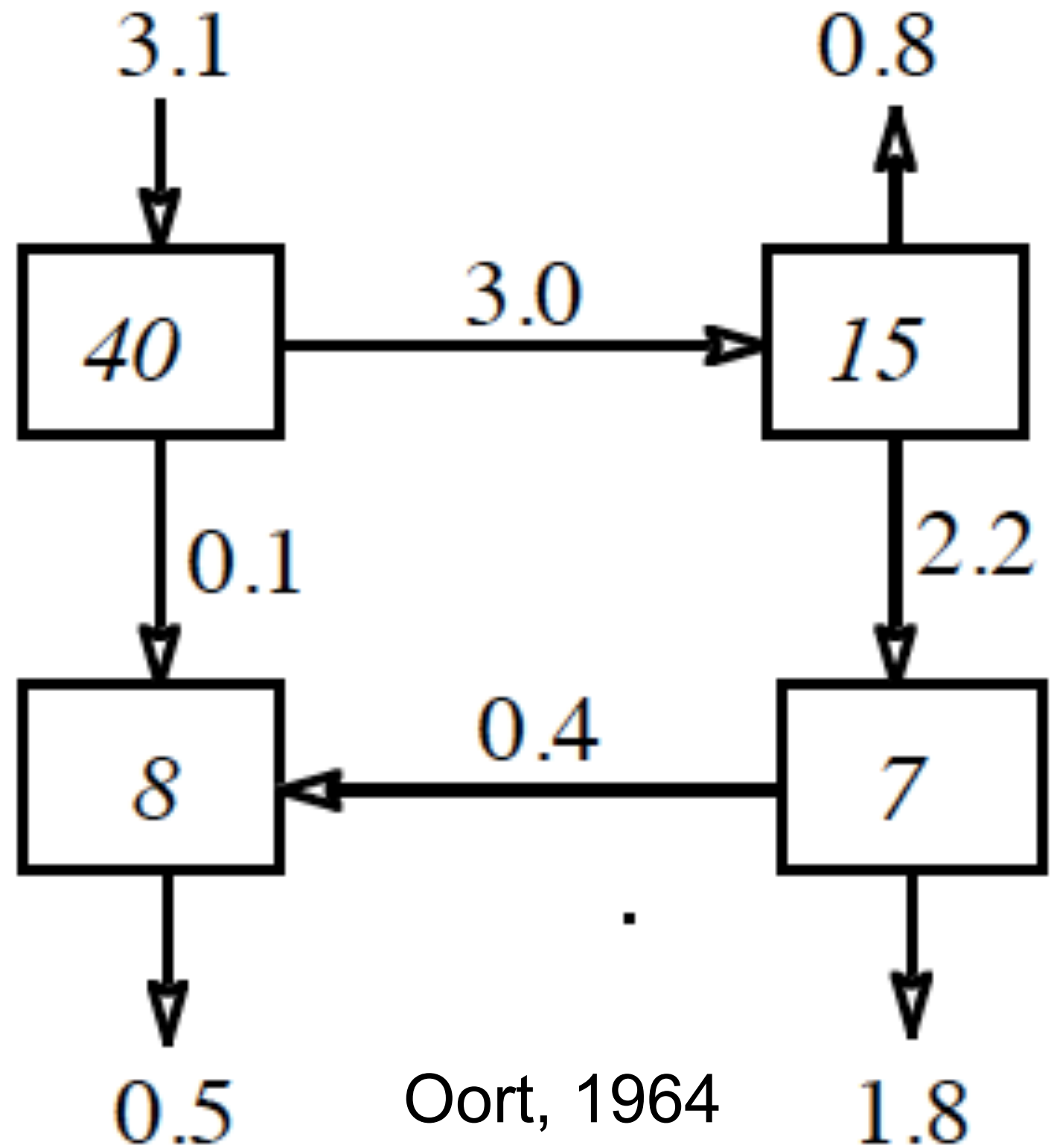
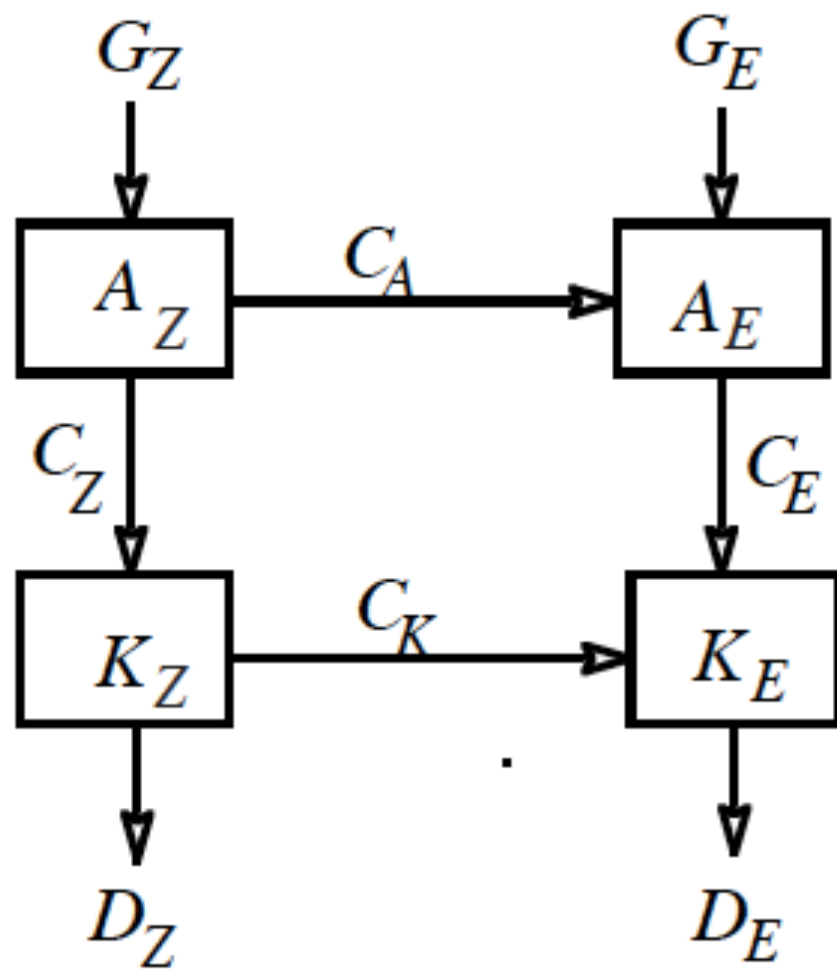
isotherms



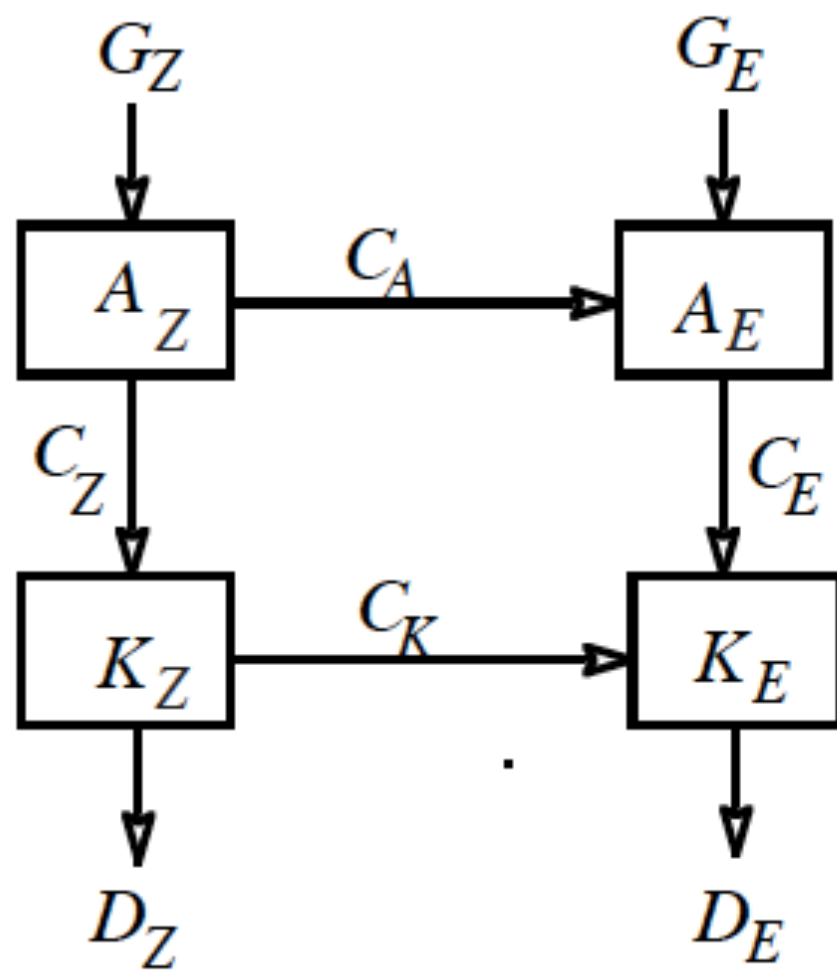
streamlines

note how the flow is amplifying the waves in the isotherms

Now let's do the numbers!



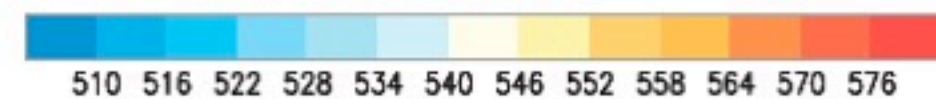
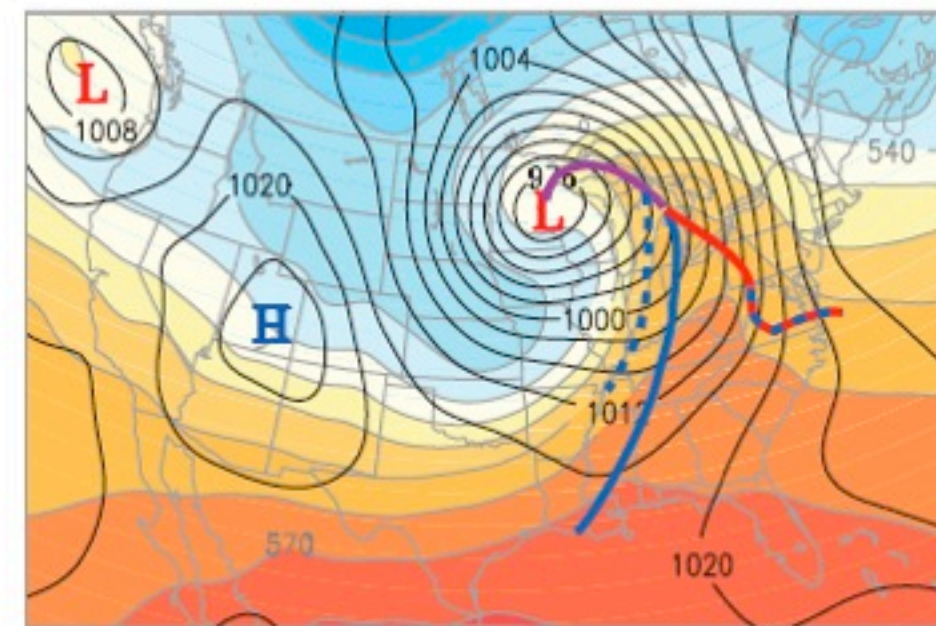
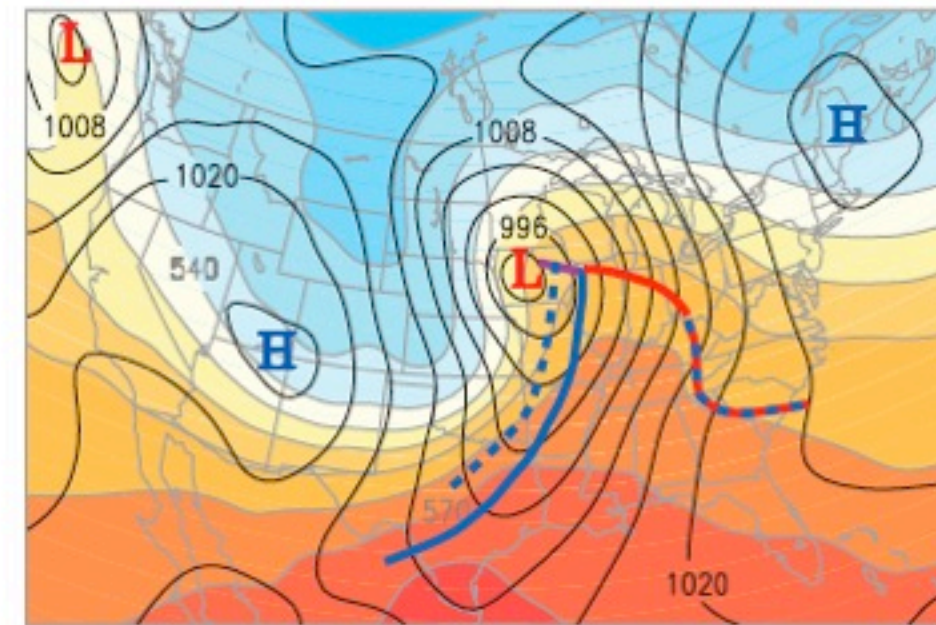
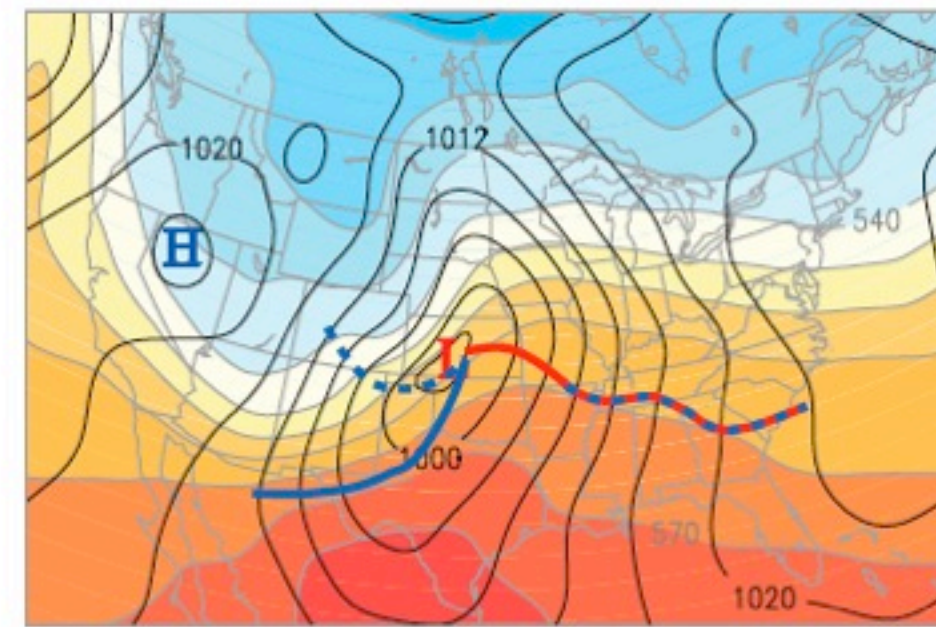
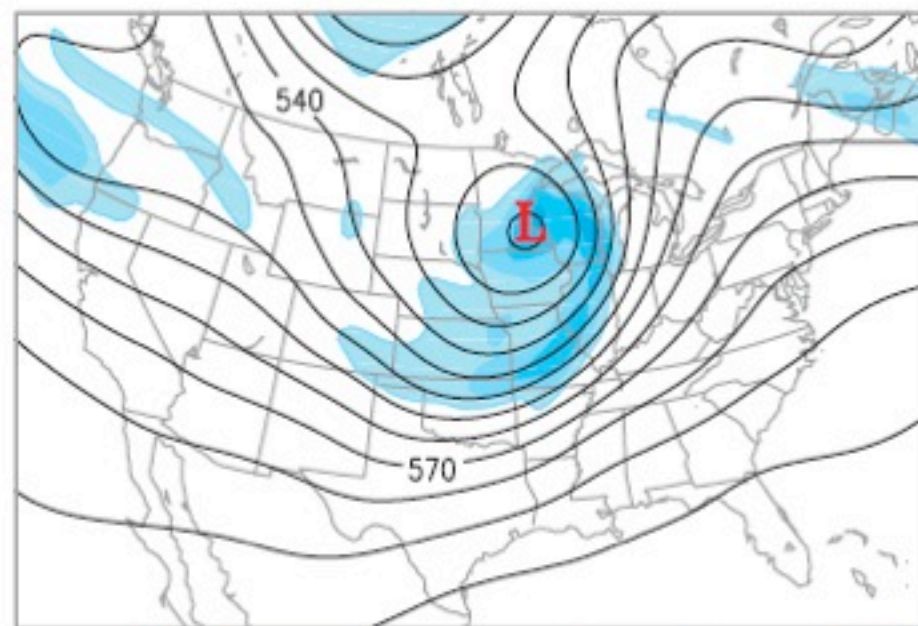
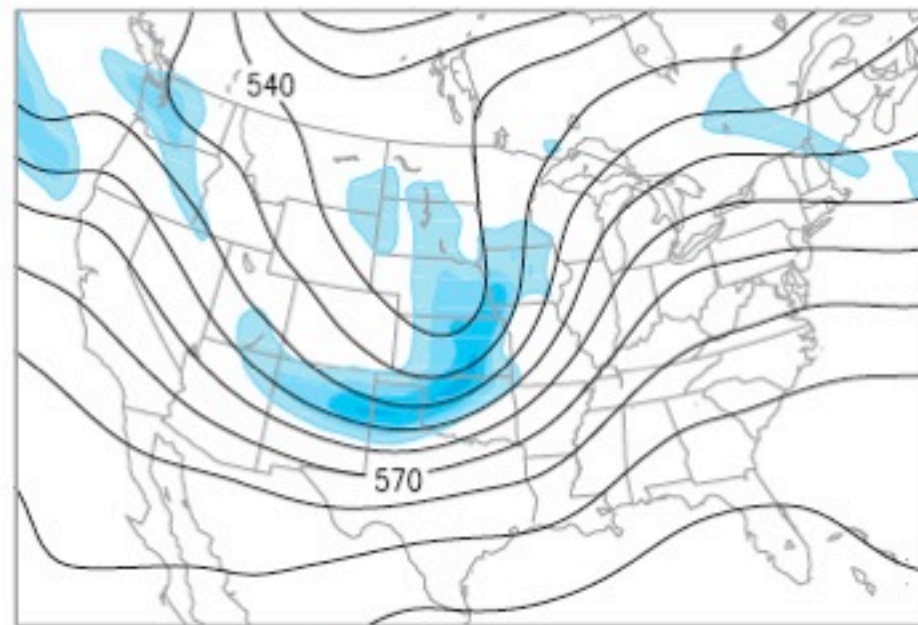
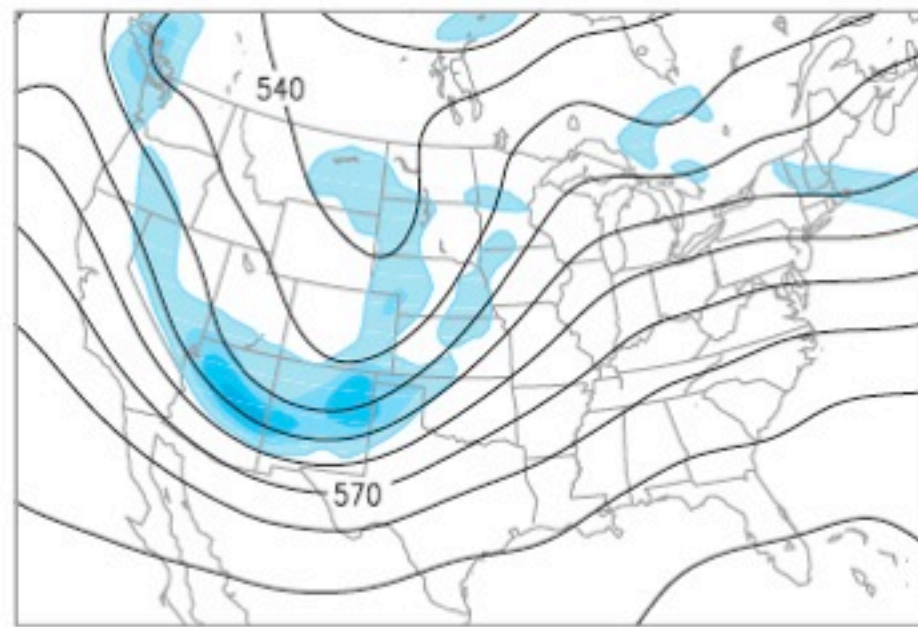
Oort, 1964



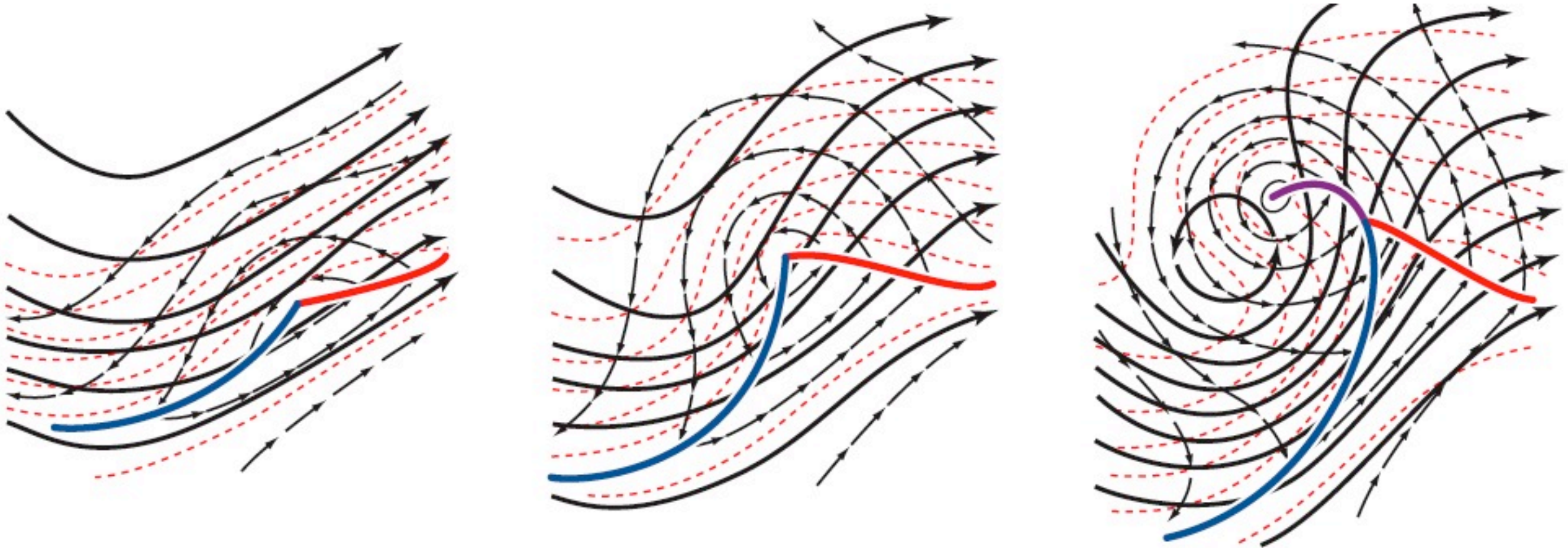
Tell us more about baroclinic waves and the KE cycle

Case Study

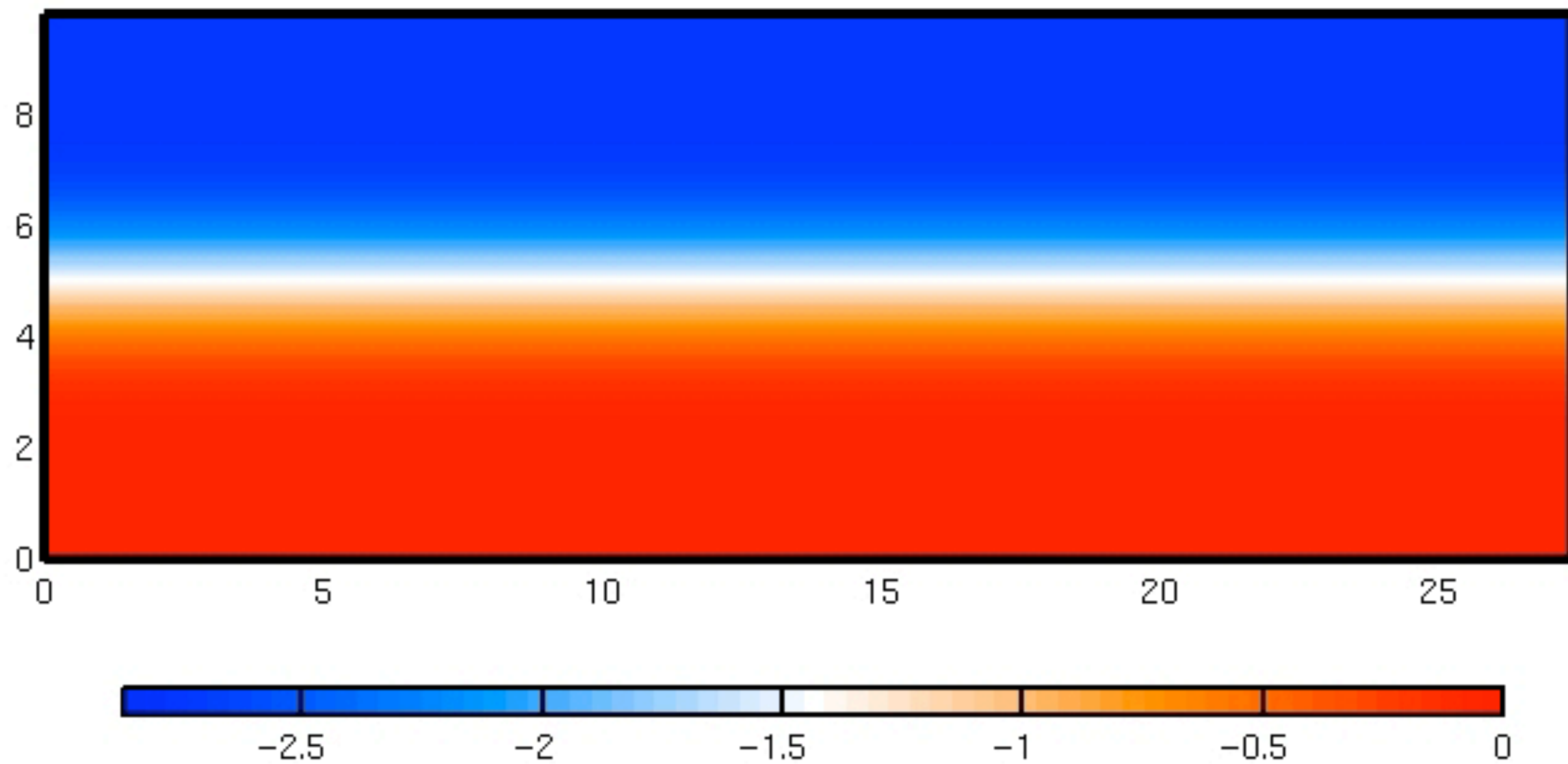
Nov. 10, 1998

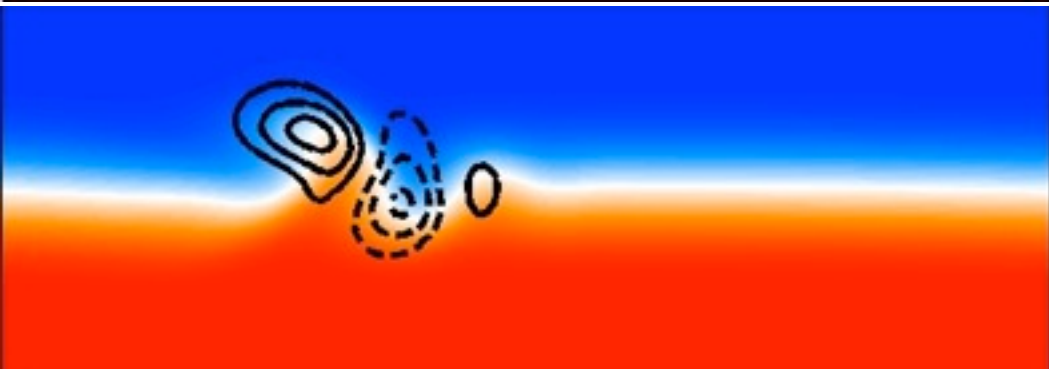
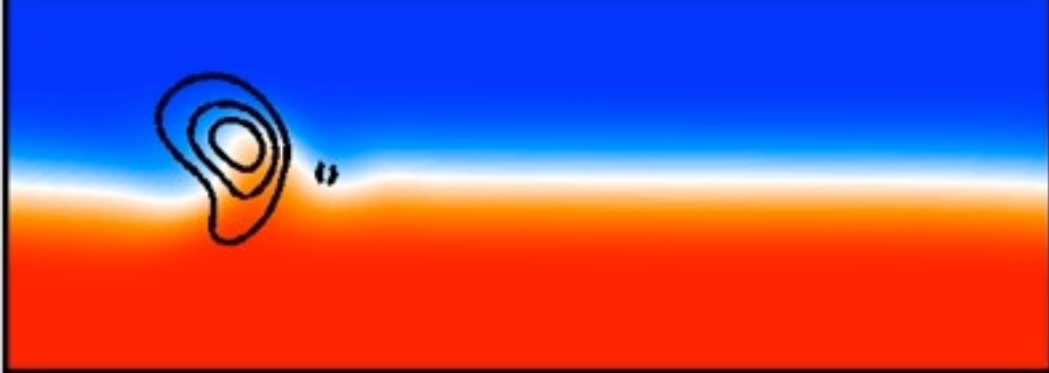


Idealized model

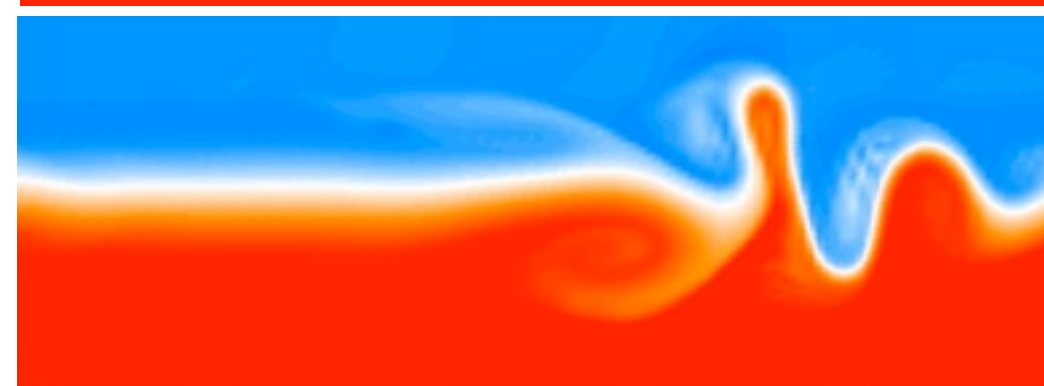
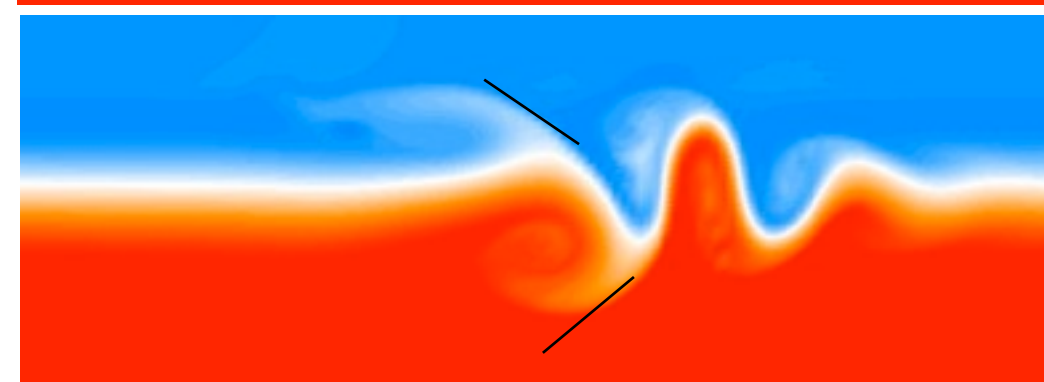
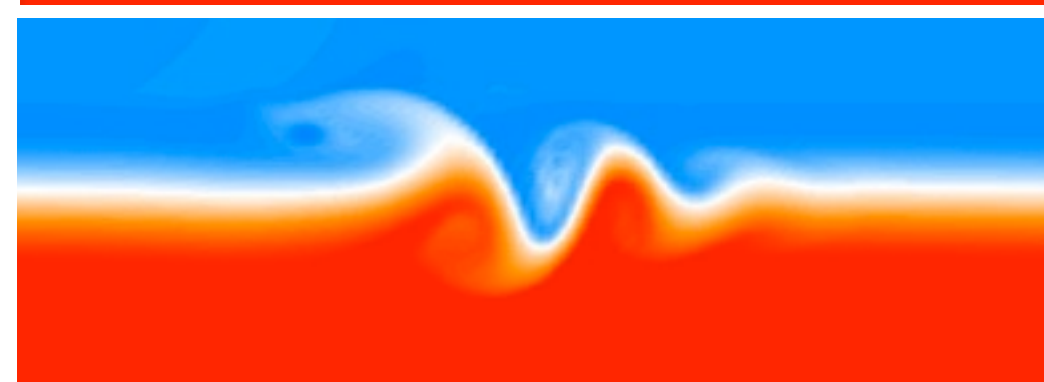
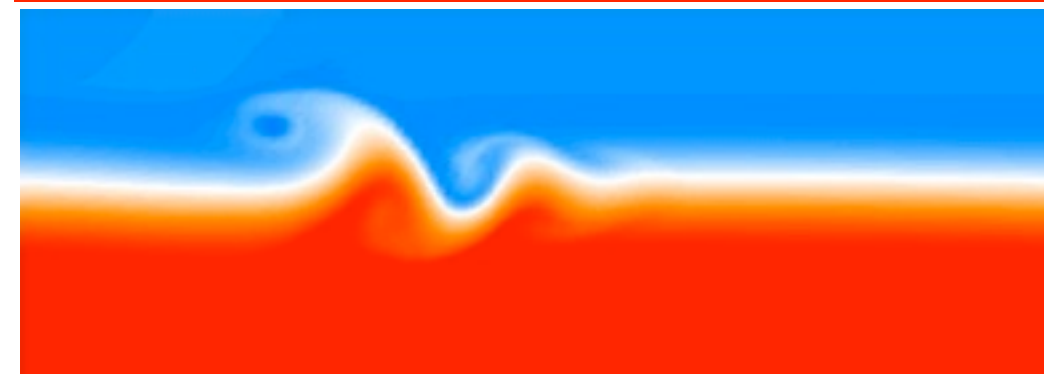


Surface Theta & Pressure...0



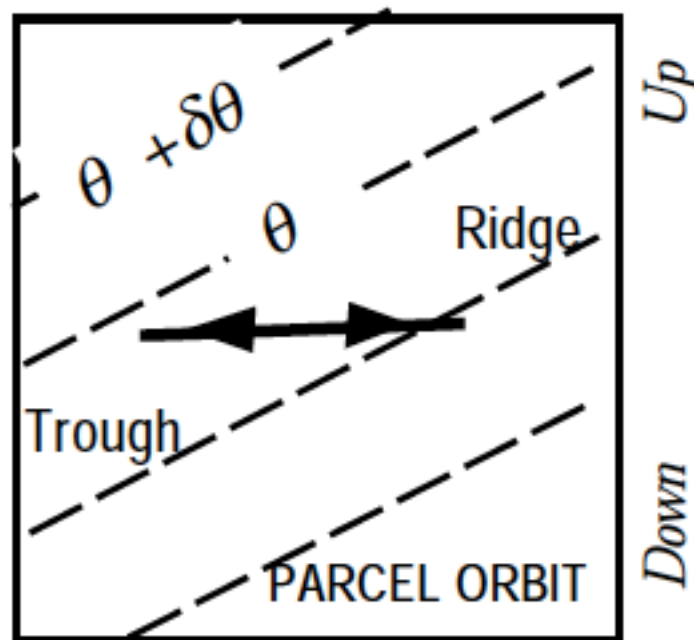


T sfc, SLP

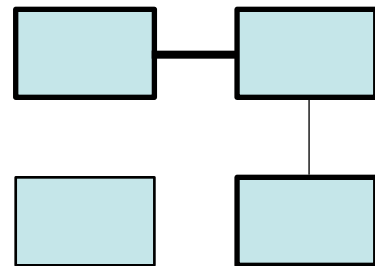


Theta on tropopause

KE cycle in developing baroclinic waves



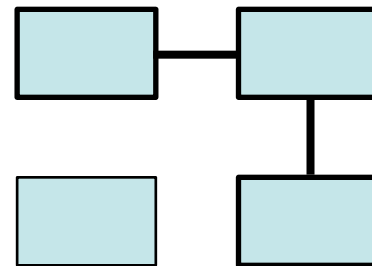
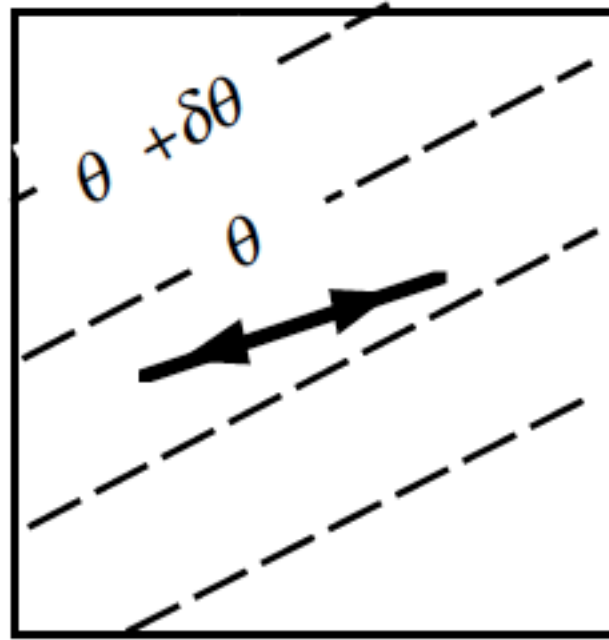
Equator Pole



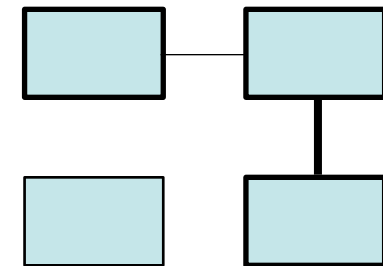
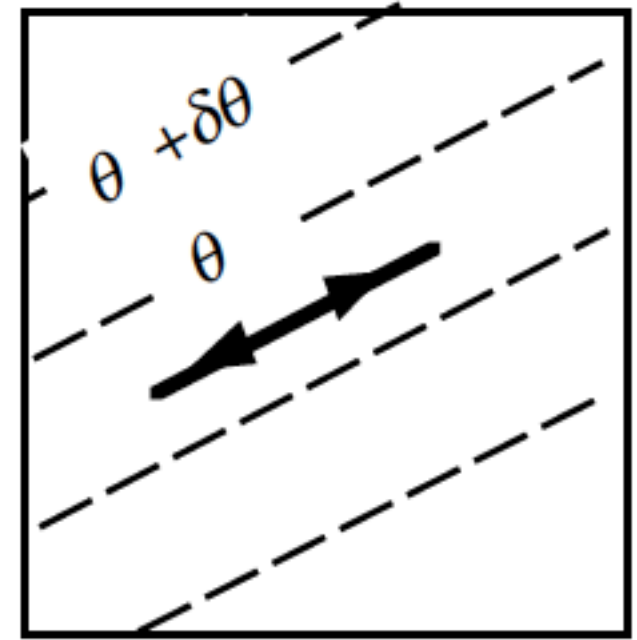
A_E generated

but little K_E

waves too long



waves just right



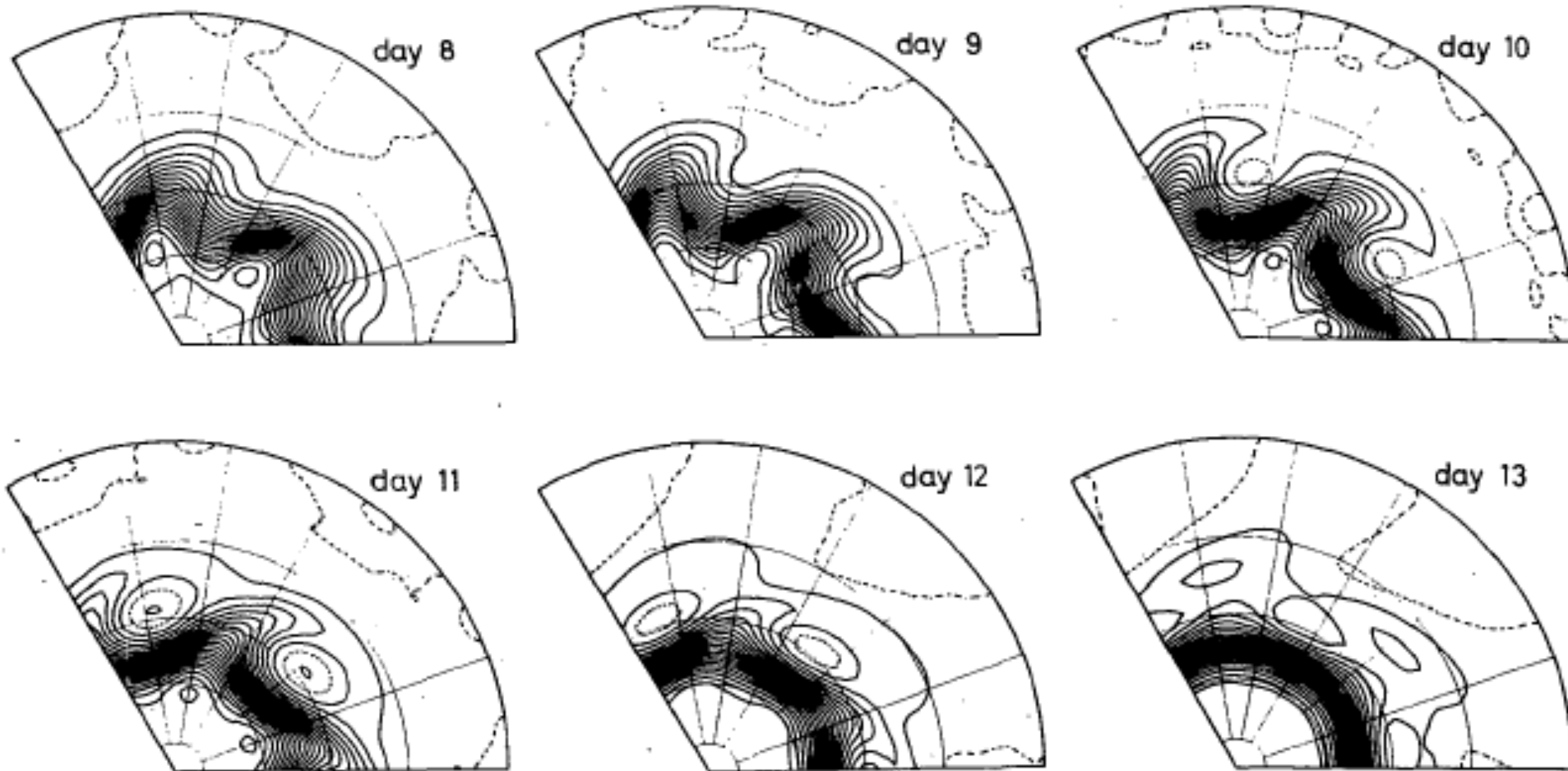
K_E generated

but little A_E

waves too short

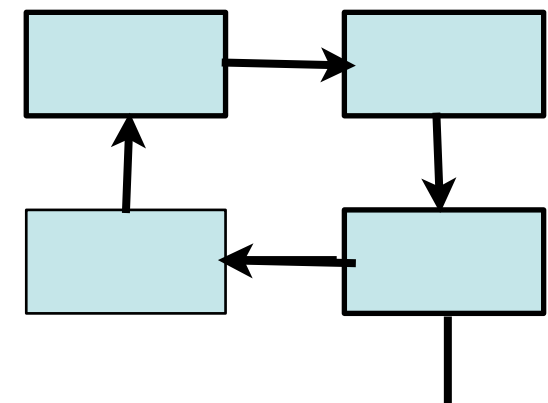
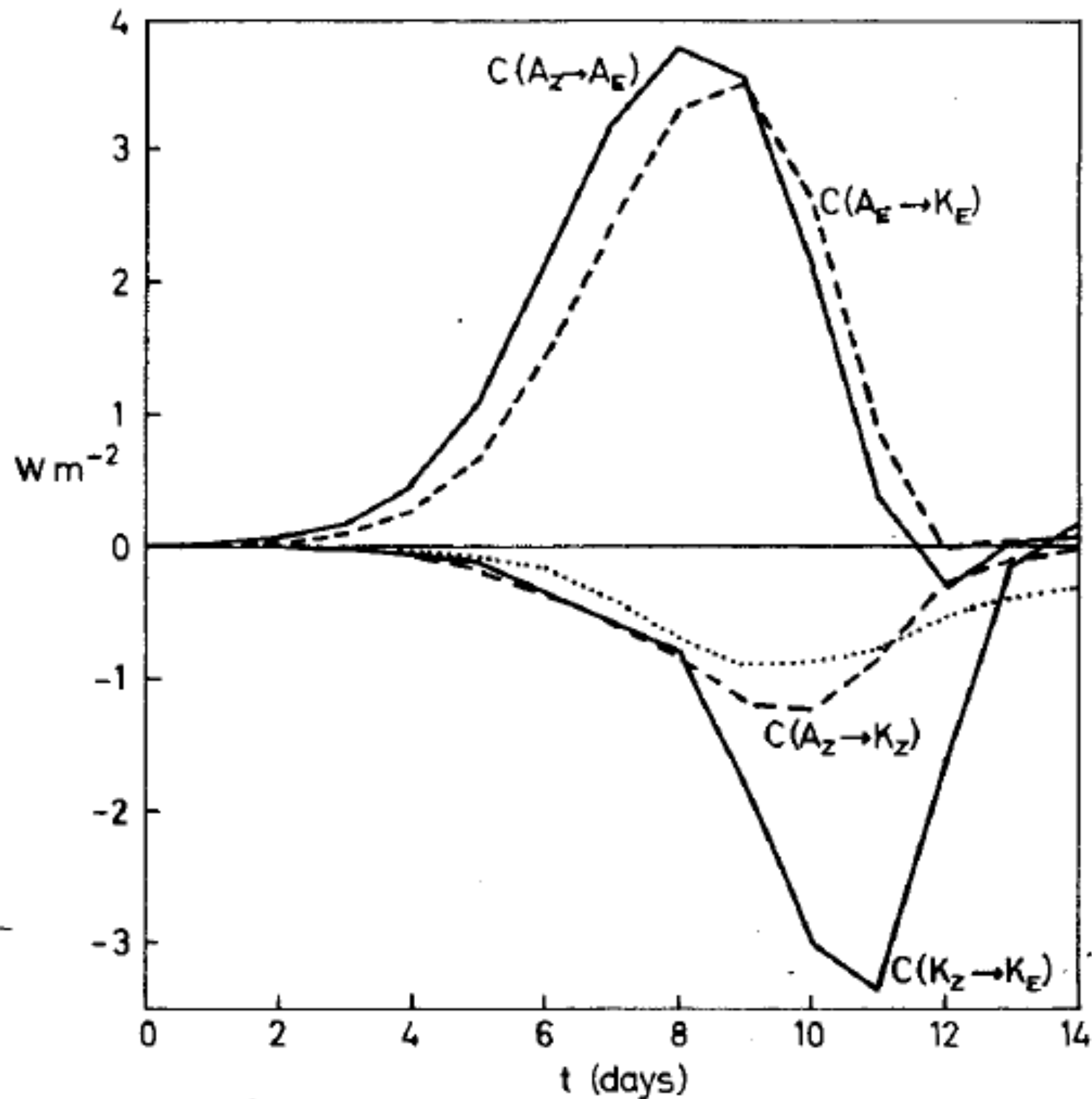


300 hPa streamfunction



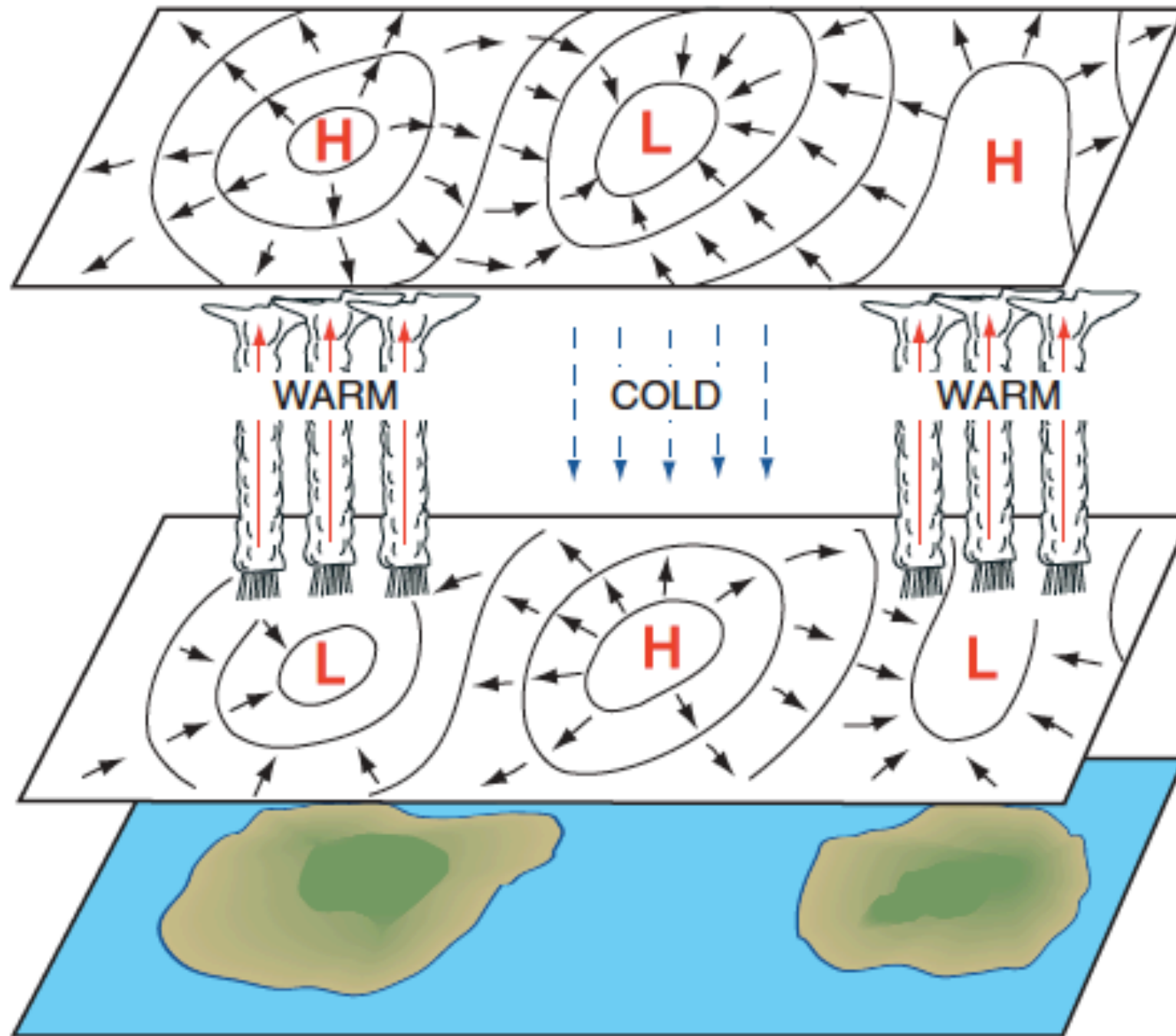
Simmons and Hoskins, JAS, 1978
idealized life cycle experiments

KE cycle in baroclinic wave life cycle



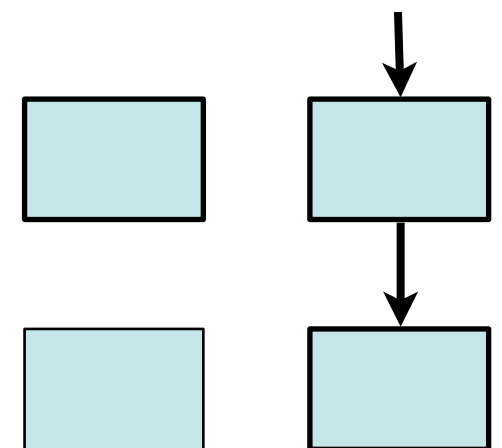
Simmons and Hoskins, JAS, 1978

KE cycle of the monsoons

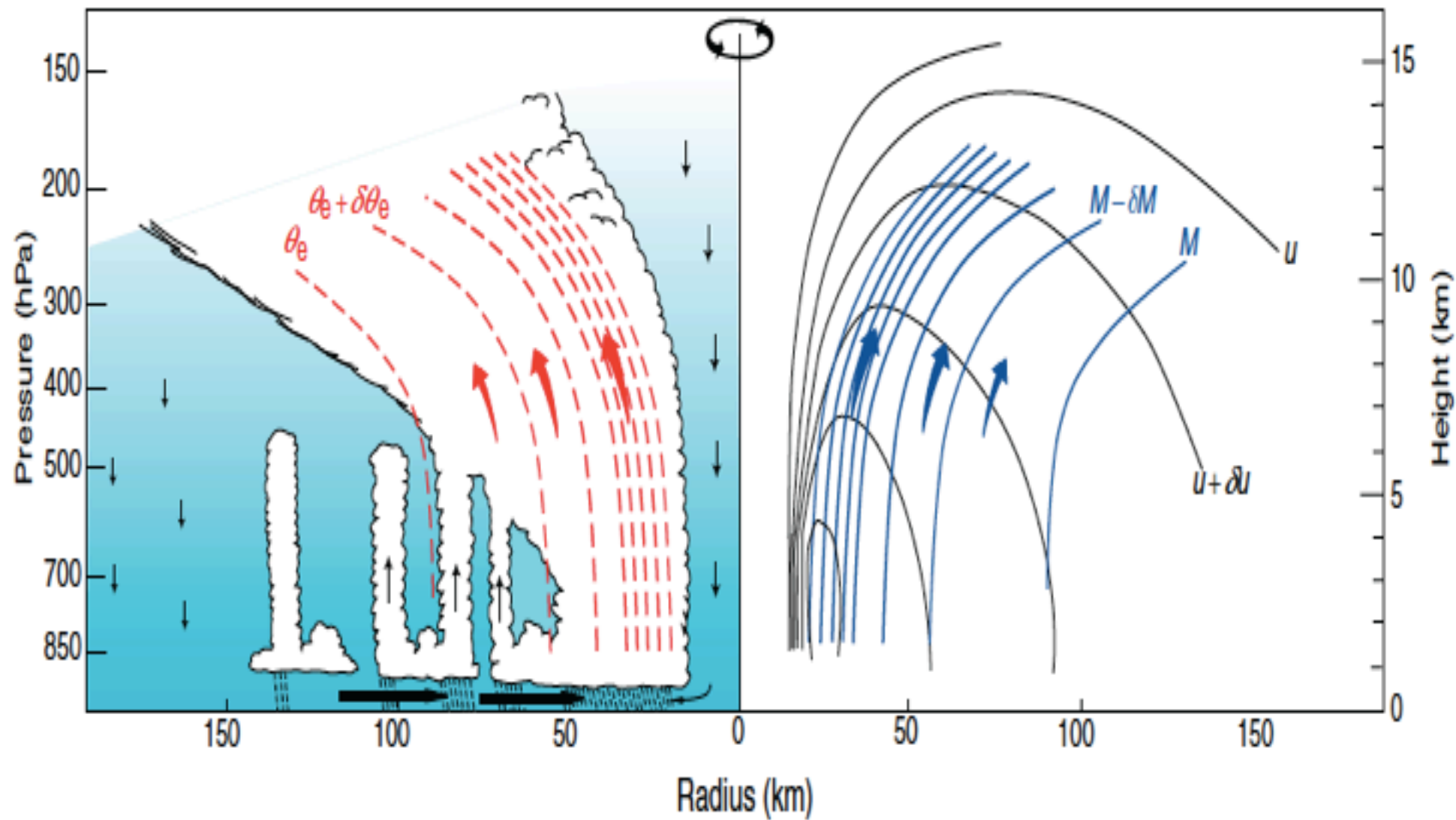


$$[Q^*T^*] > 0$$

$$[\omega^*T^*] < 0$$

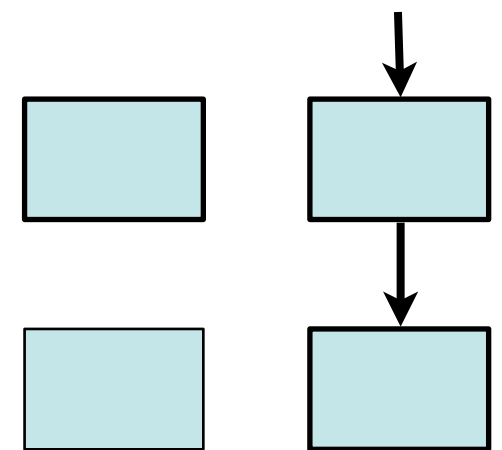


KE cycle of tropical cyclones

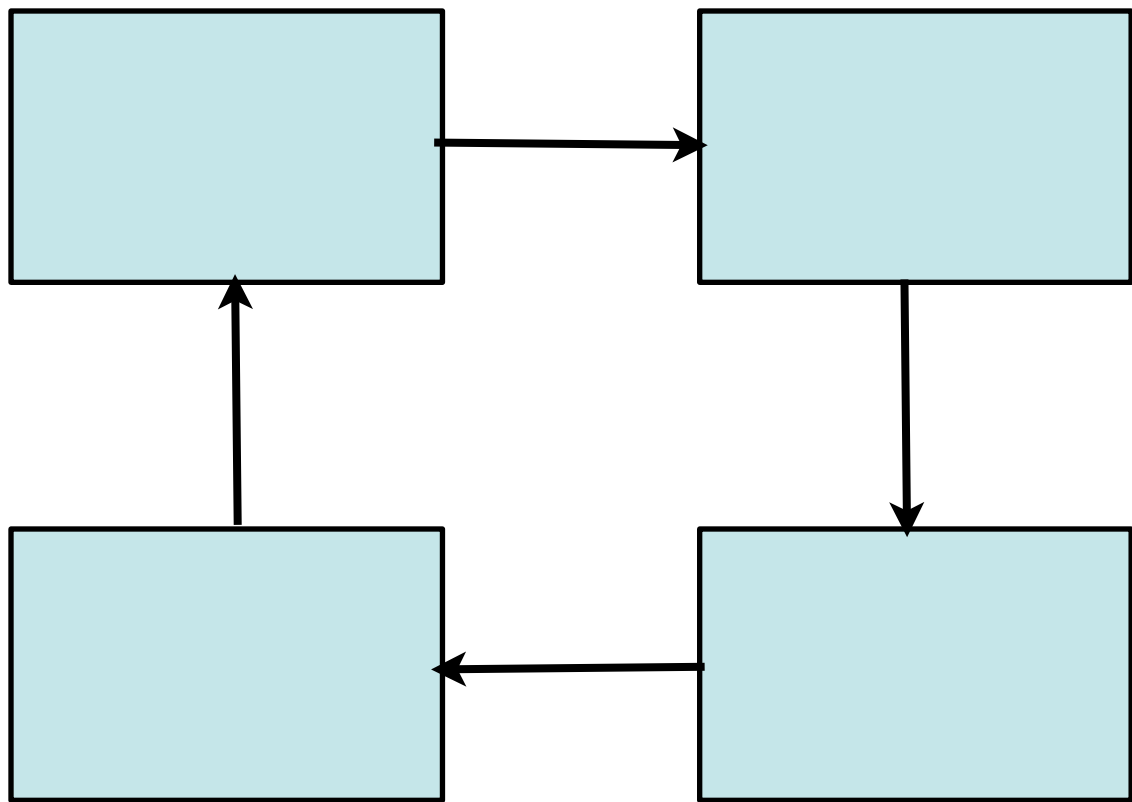


$$[Q^*T^*] > 0$$

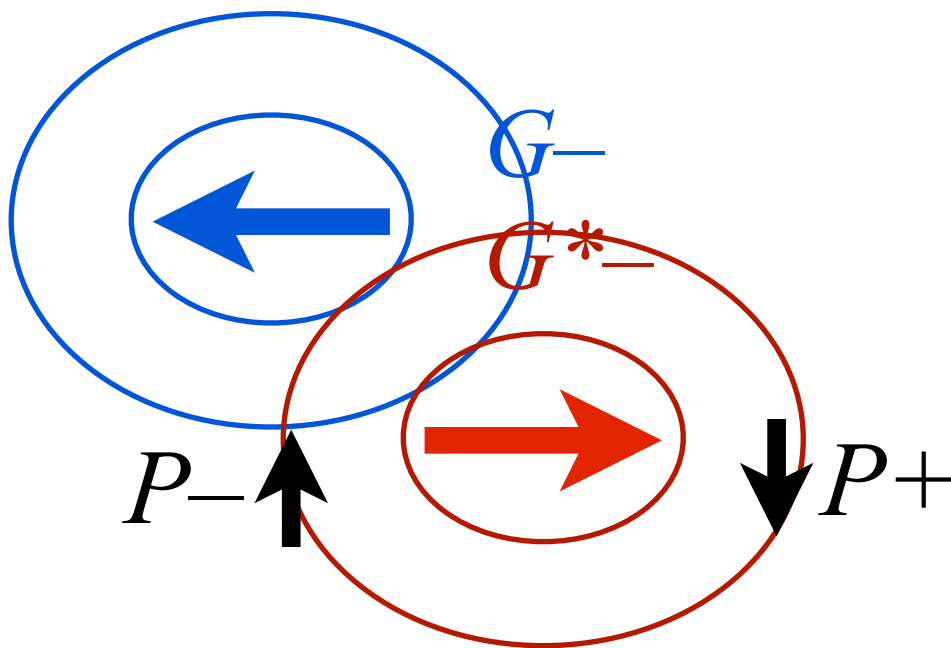
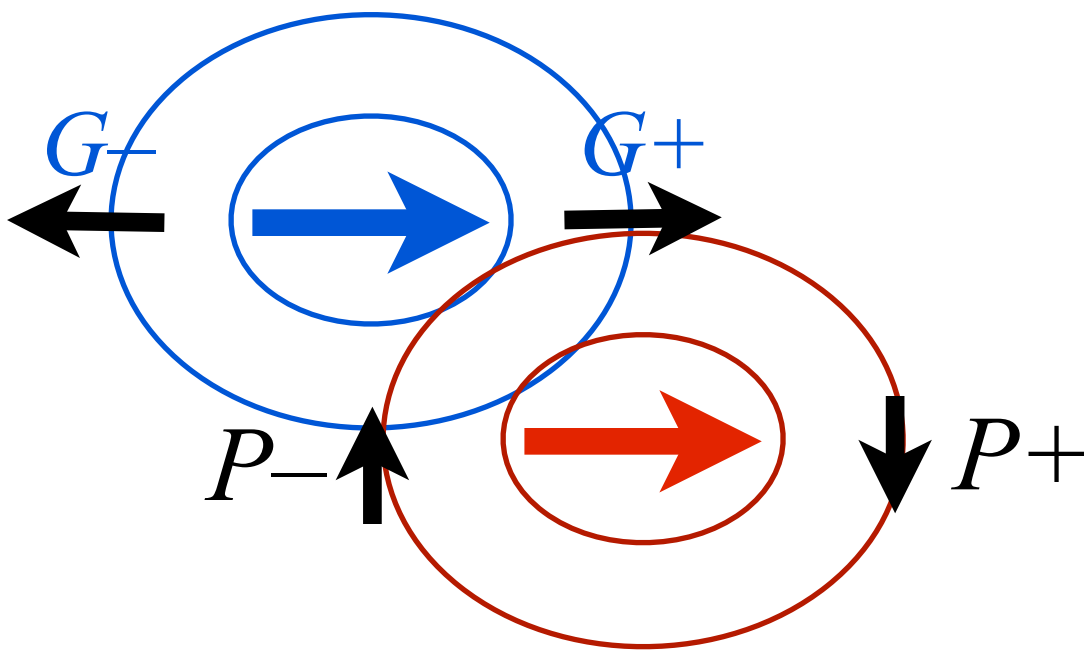
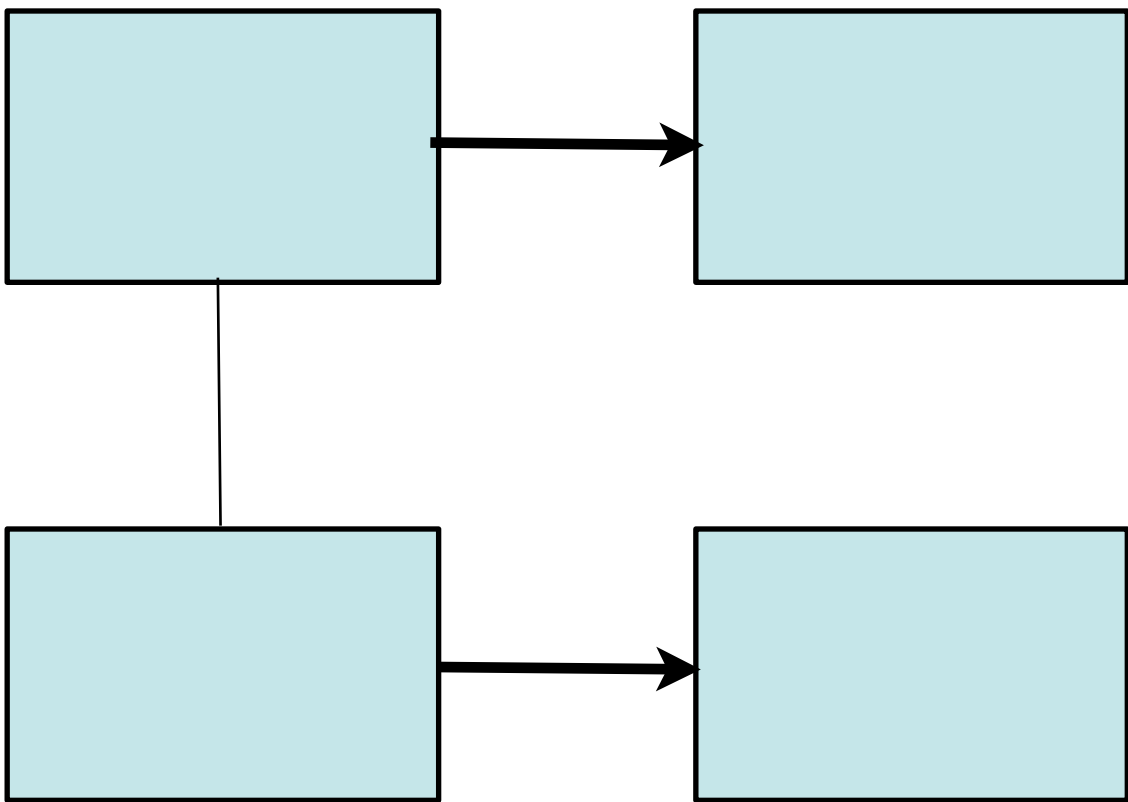
$$[\omega^*T^*] < 0$$



1. Quiescent regime with strong jet

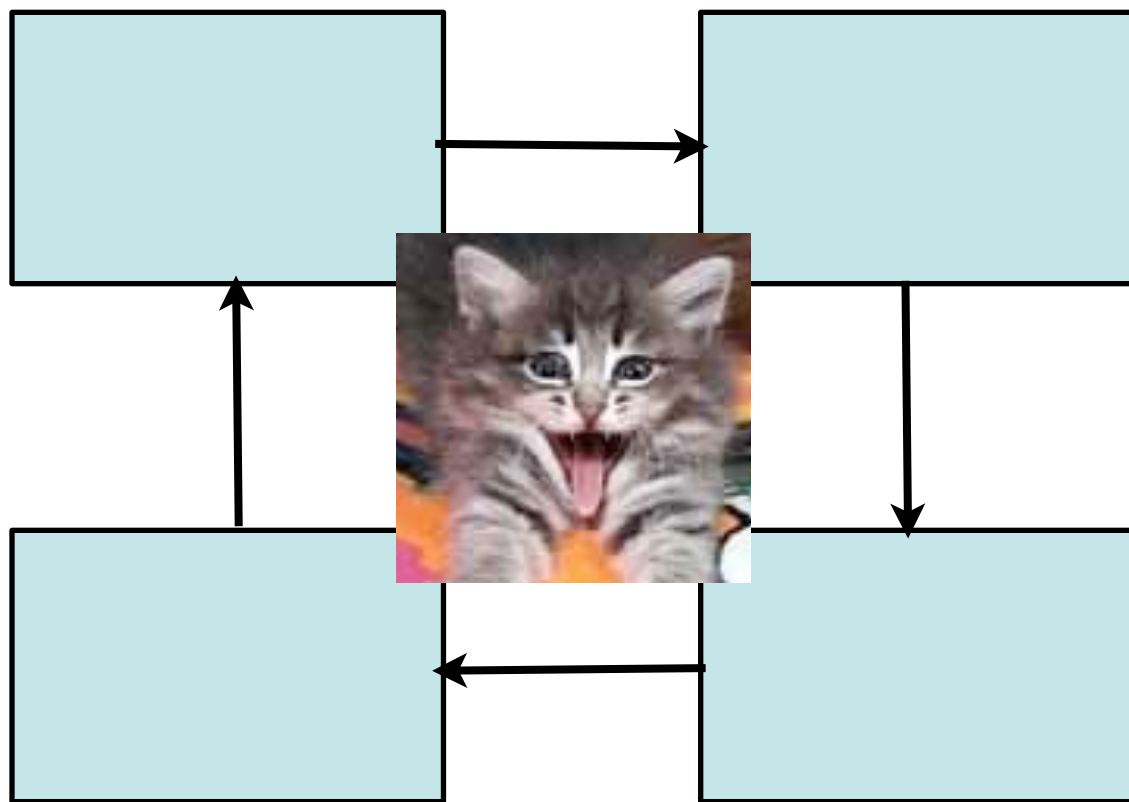


2. Sudden warming



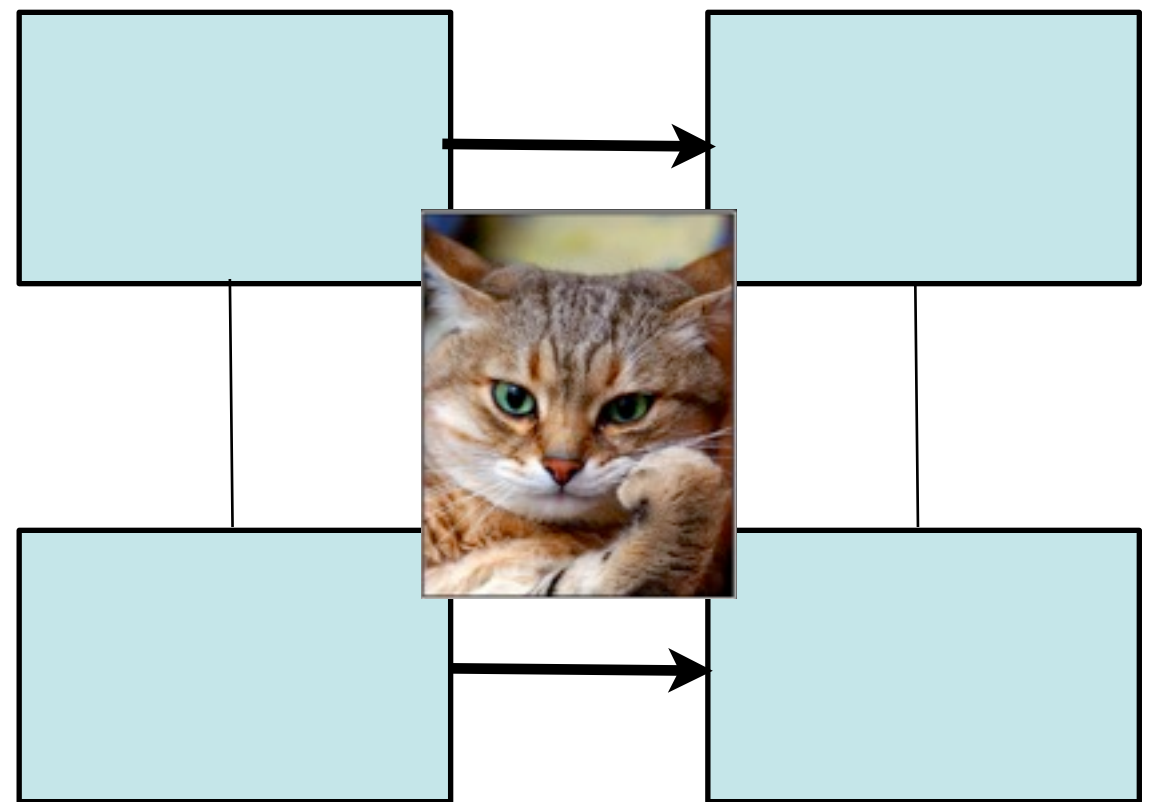
KE cycle in the stratosphere

1. Quiescent regime with strong jet



awesome conversions
but nothing happens

2. Sudden warming



the MMC stand by idly
and let the jet collapse