

# GFD I

Frierson

Lecture 4: 1-11-17

# Last time...

- Convective instability
  - Convective instability criteria for atmos and ocean:

$$\frac{\partial \rho \theta}{\partial z} > 0 \quad (\text{ocean})$$

$$\frac{\partial \theta}{\partial z} < 0 \quad (\text{atmosphere})$$

# Last time...

- Static stability:
  - If stable, parcels oscillate up and down w/ frequency

$$N = \left( -\frac{g}{\rho_\theta} \frac{\partial \rho_\theta}{\partial z} \right)^{(1/2)} \quad (\text{ocean})$$

$$N = \left( \frac{g}{\theta} \frac{\partial \theta}{\partial z} \right)^{(1/2)} \quad (\text{atmos})$$

# Moisture

- New variable: equivalent potential temperature

$$\theta_e = \theta \exp \left( \frac{L_v q}{c_p T} \right)$$

- If parcel is saturated,  $\frac{\partial \theta_e}{\partial z}$  determines stability.
- $\theta_e$  is conserved whether saturated or not!

# A few other moisture definitions

- Clausius-Clapeyron equation for saturation vapor pressure:

$$e_s = e_{s0} \exp \left( -\frac{L_v}{R_v} \left( \frac{1}{T} - \frac{1}{T_0} \right) \right)$$

$$R_v = 461.5 \text{ J/kg/K}$$

$$e_{s0} = 611 \text{ Pa if } T_0 = 273.16 \text{ K}$$

$$L_v = 2.5 \times 10^6 \text{ J/kg}$$

- Specific humidity equation:  $q = \epsilon \frac{e}{p}$

$\epsilon = 0.62$  = ratio of mass of water vapor to dry air

# Today

- Sound waves
- Incompressibility
- Advection-diffusion