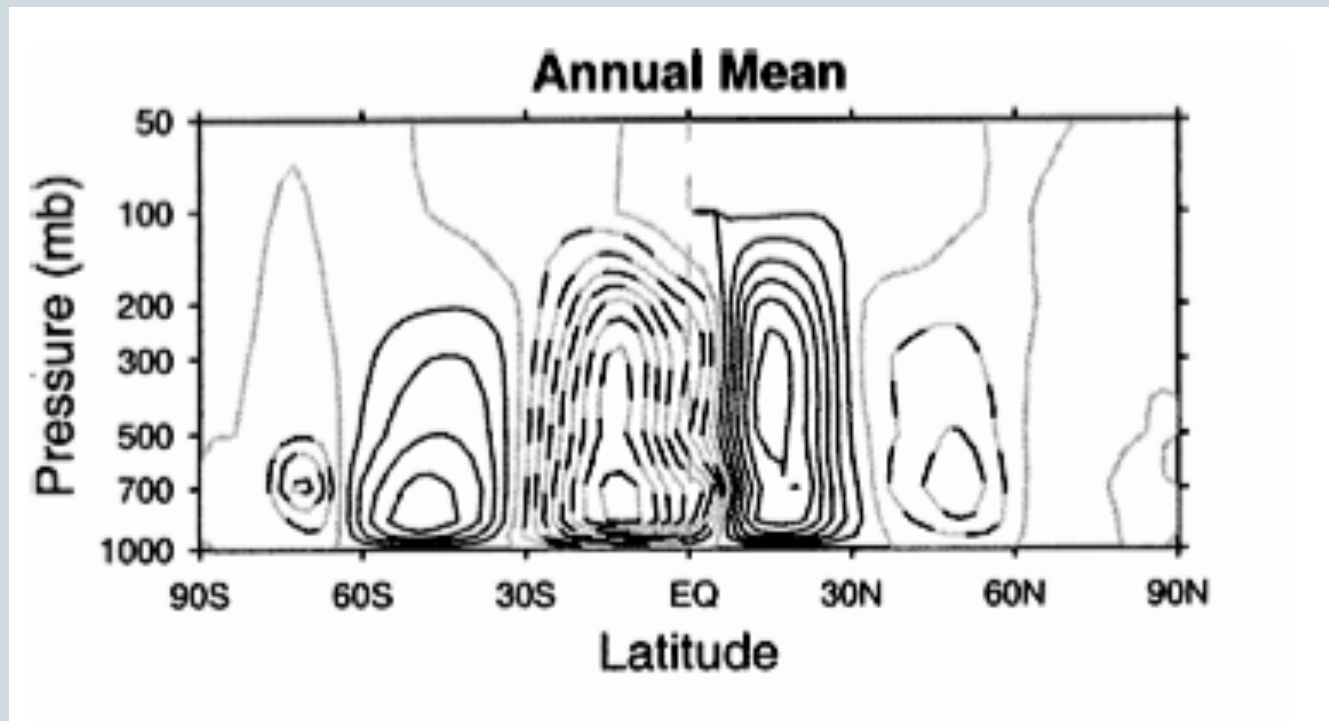


Hadley cell observations



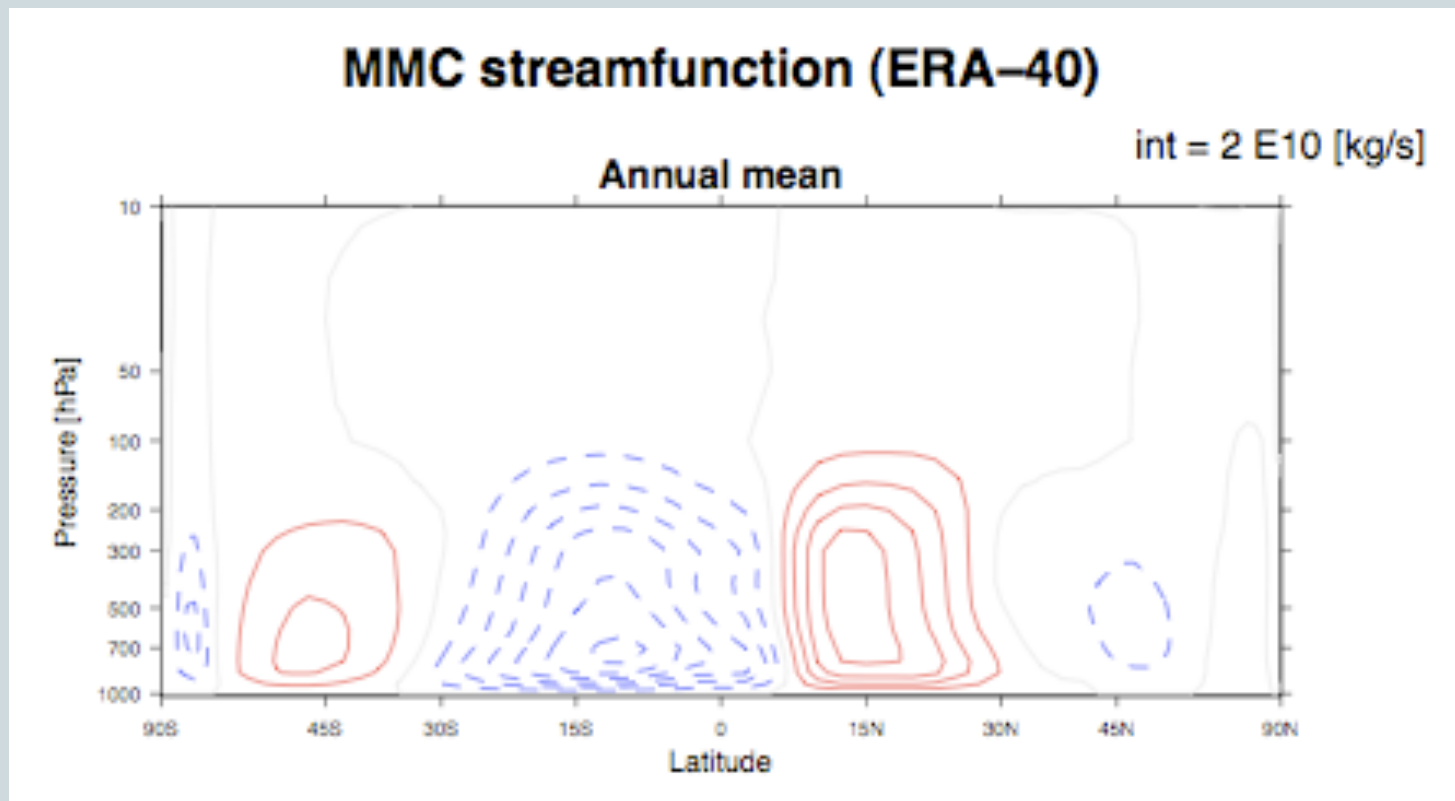
- NCEP reanalysis (Dima and Wallace 2003):



Hadley cell observations



- ERA-40 reanalysis (Rei Ueyama):



$\sin(\text{latitude})$

Momentum Equation Derivations...



- Held-Hou theory for Hadley cell
 - Zonal momentum budget:
 - ✦ Angular momentum conservation
 - ✦ Winds reach very strong speeds quickly: e.g., $u=95 \text{ m/s}$ at 25 deg
 - Meridional momentum equation:
 - ✦ Geostrophic balance
 - One of the ignored terms was $v \, dv/dy$: assumed small relative to $f \, u$ because $v \ll u$
 - ✦ Thermal wind in meridional direction then gives you temperatures
 - Really small temperature gradients
 - 0.6 K at 12 deg, 3.2 K at 18 deg

Next...

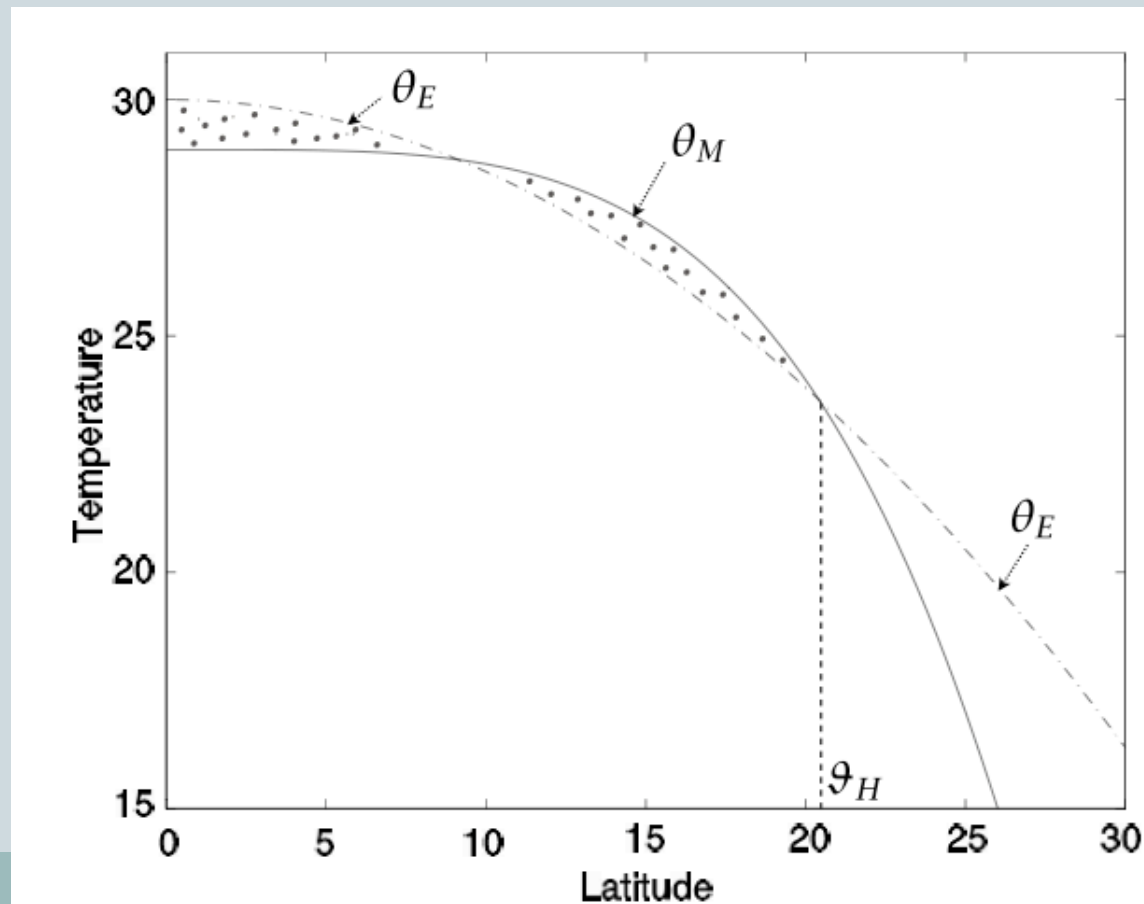


- **Thermodynamics:**
 - To close the problem & solve for width, strength, etc
- **First assume Newtonian cooling, as in Held-Suarez model**

“Equal-area” argument



- Conservation of energy:



Held-Hou Results

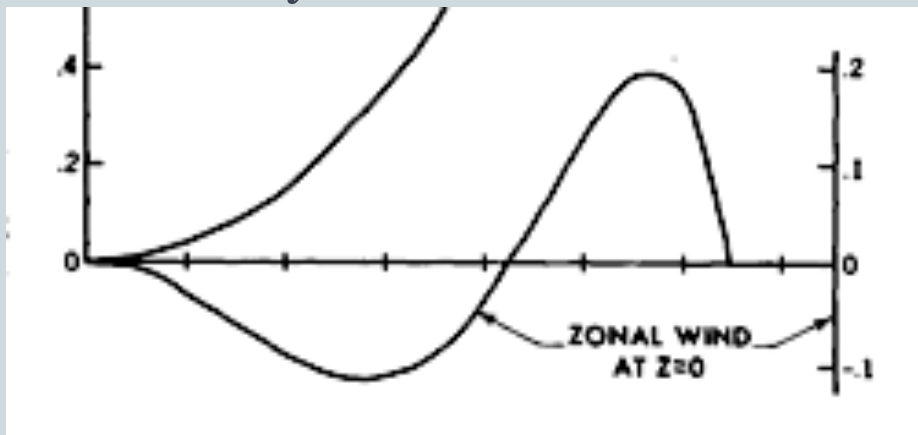


- Width is proportional to:
 - Square root of equilibrium temperature gradient
 - Square root of height of tropopause
- Inversely proportional to:
 - Rotation rate

Held-Hou Results



- Strength proportional to:
 - “Area” in equal area argument (distance from equilibrium profile)
- Strength inversely proportional to:
 - Radiative relaxation time
 - Static stability



Surface winds

Held-Hou Criticism

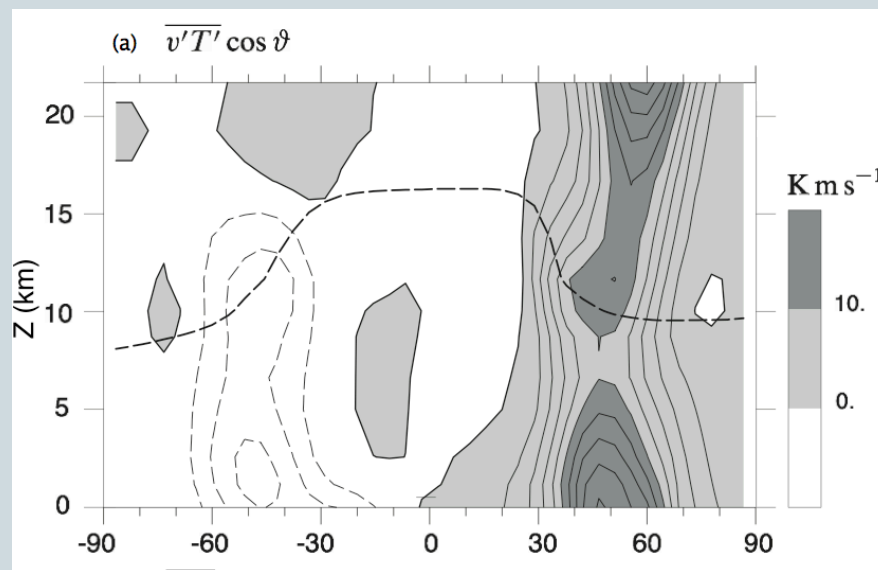


- Rough comparison with observations:
 - Good:
 - ✦ Right width
 - ✦ Surface winds right sign in right places
 - Bad:
 - ✦ Upper tropospheric winds way too strong
 - ✦ Circulation too weak
 - Ugly:
 - ✦ Radiative equilibrium outside the cell
 - ✦ Impossible to get surface winds outside the cell



Ways to Fix Problems?

- Can use a radiative-convective-**eddy** equilibrium temperature profile:
 - Eddies cool the subtropics, warm the higher latitudes

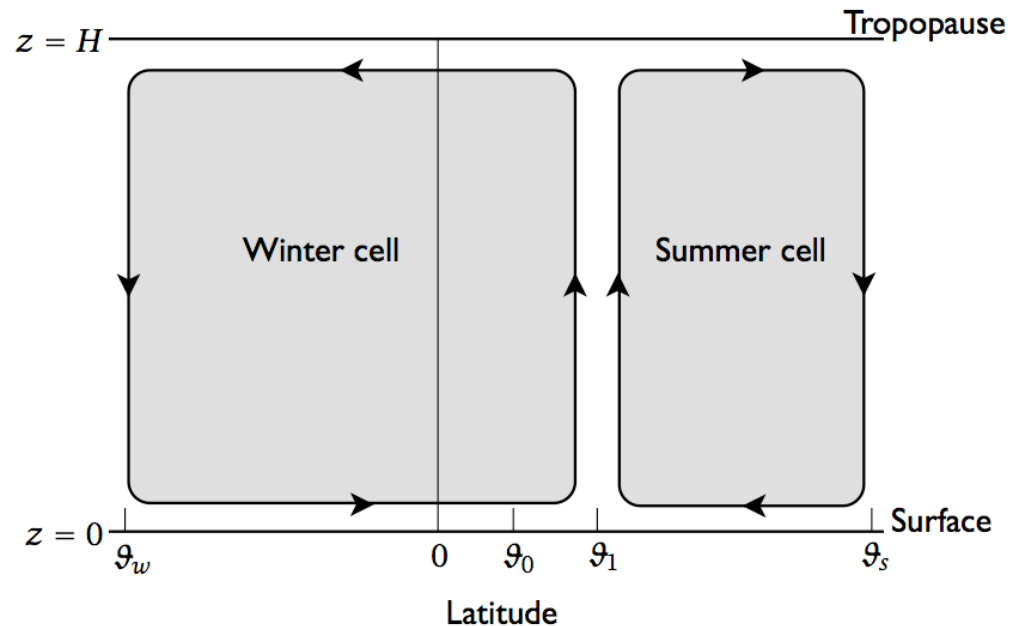


- Would result in a stronger circulation
 - ✦ Cooling subtropics increases gradients within the Hadley cell

Extensions to Held-Hou Model



- Lindzen & Hou (1988): forcing asymmetric about the equator
 - Can predict boundary between cells, cell widths, & cell strengths
 - ✦ ITCZ location (location of maximum heating) is specified in this problem
 - ✦ Boundary b/w cells is poleward of “ITCZ”



Extensions to Held-Hou Model

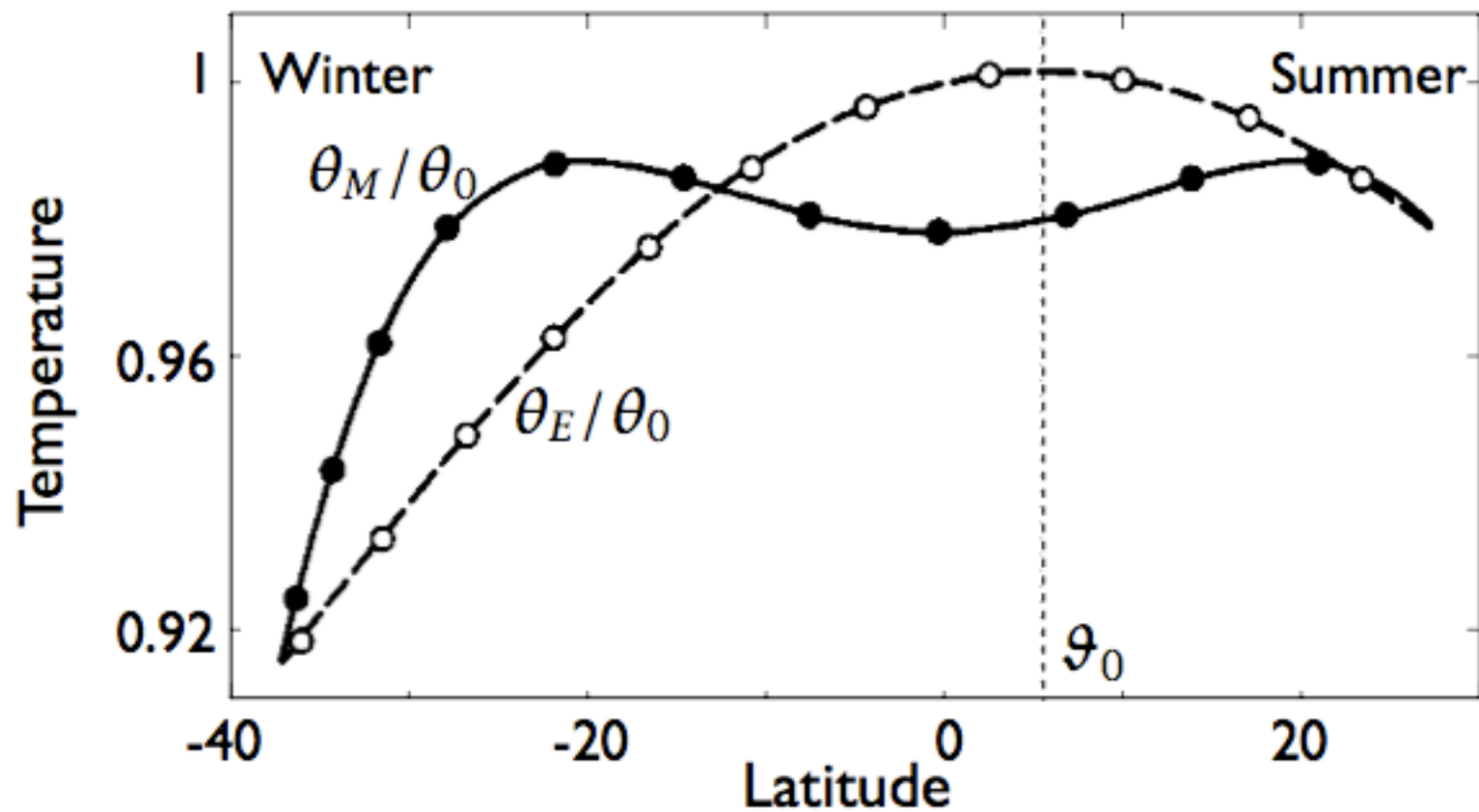


- Lindzen & Hou (1988): forcing asymmetric about the equator
 - Asymmetry is very large between summer and winter hemispheres
 - ✦ As in observations
 - Derivation: wind and temperature structure when forcing is off-equator (on the board)

Asymmetric Hadley cell



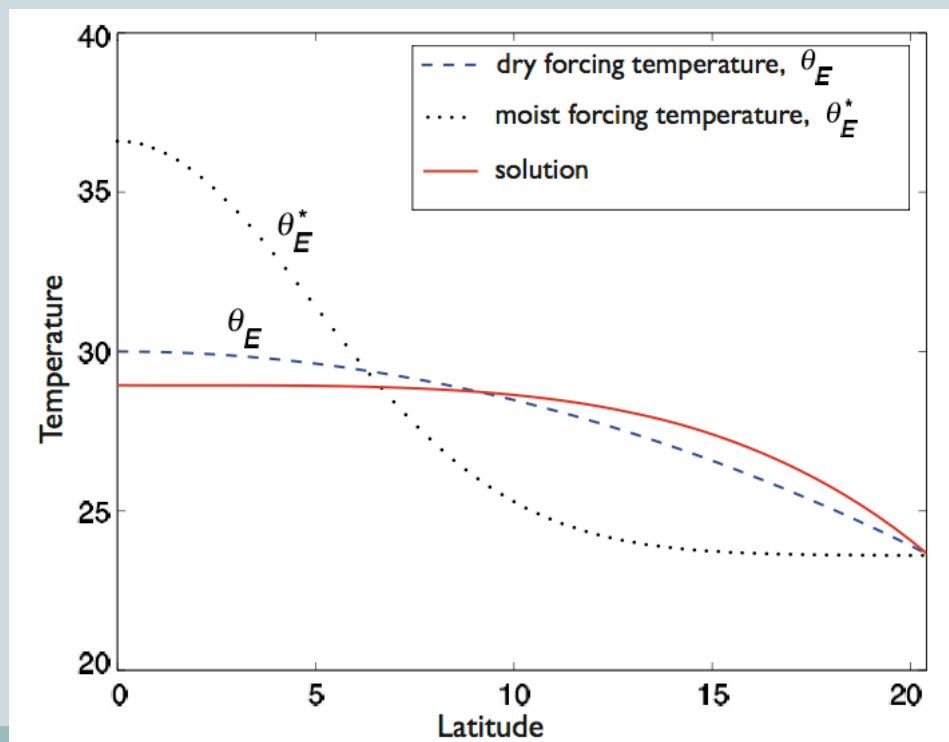
- Temperatures:



Extensions to Held-Hou Model



- Hou & Lindzen (1992): localized forcing
 - Delta-function (or highly concentrated) forcing: “ITCZ”
 - Basic idea described in Vallis



Extensions to Held-Hou Model



- Hou & Lindzen (1992): localized forcing
 - Gives stronger circulation (obviously)
 - Dangerous way to put in moisture
 - ✦ Might expect stronger circulation with more moisture/heating
 - ✦ However, one of the main things moisture does is change static stability: actually can get significantly weaker circulation with higher moisture contents with this effect
 - Models with active moisture budgets are preferable

Extensions to Held-Hou Model



- Fang and Tung (1996, 1997, 1999):
 - Analytic solutions w/ viscosity, vertical structure, etc
 - Changes with thermal relaxation time
 - Time dependent circulations

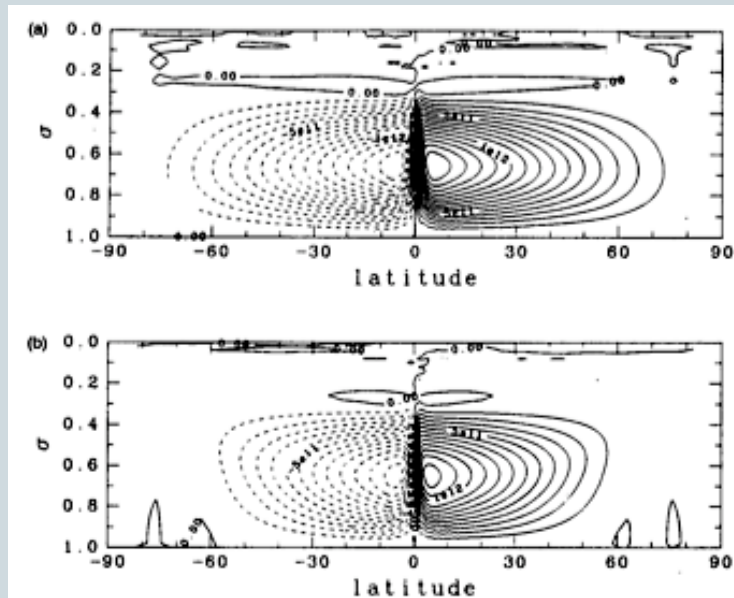
EYEBall/skeleton



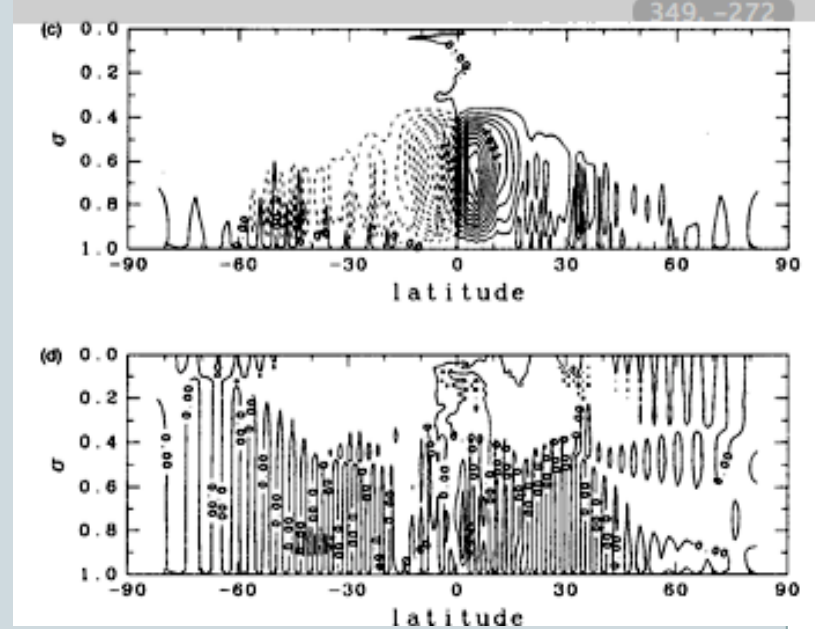
Adding moisture

- Satoh (1994): moisture
 - Ran simulations with a moist axisymmetric model (gray radiation, etc)
 - Developed theory for this

$\Omega = 0.1 \times \Omega_E$



$\Omega = 10 \times \Omega_E$



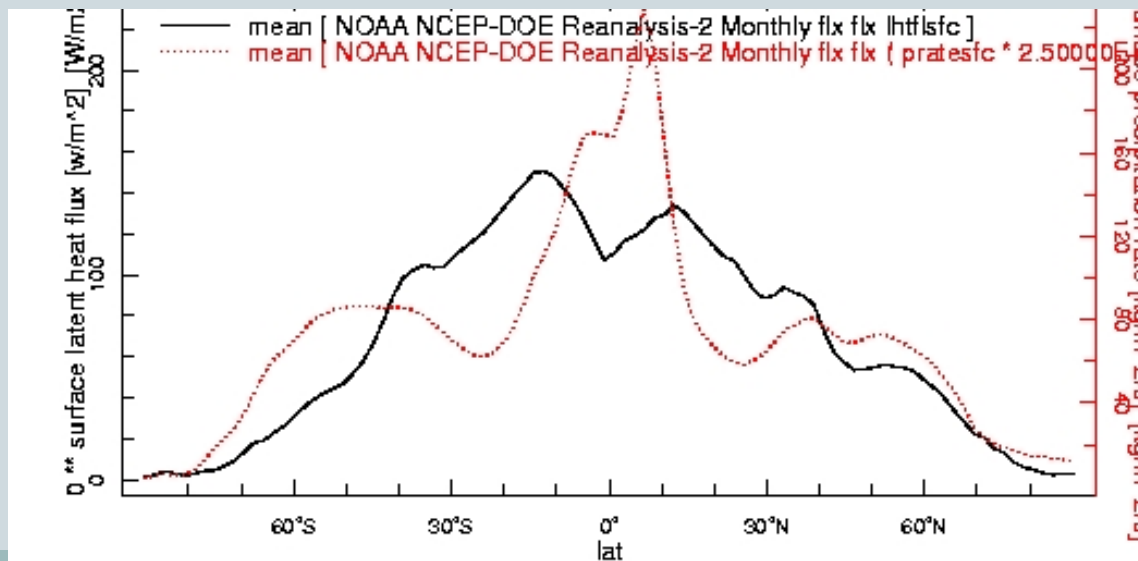
A first moist Hadley cell



- **Satoh (1994): moisture**
 - All simulations show very concentrated upward motion
 - Developed simple theory based on the axisymmetric simulations:
 - ✦ Assume localized ITCZ, dry subtropics
 - ✦ Static stability determined by moist adiabat (humidity at equator)
 - ✦ Balance between radiative cooling and subsidence in dry subtropics determines strength
 - ✦ Angular momentum conserving winds
 - ✦ Width determined by thermodynamics (as in Held-Hou)

Satoh (1994) theory

- Satoh (1994): moisture
 - Interesting way to consider the effect of moisture without an active moisture budget
 - ✦ Dry region controls everything
 - Limited applicability though? Subtropics are clearly not dry:

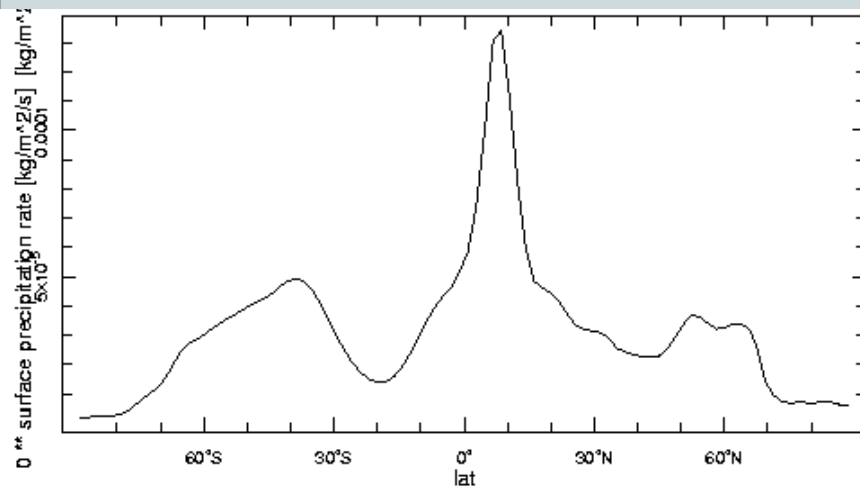


Evap and **precip**
NCEP Reanalysis 2

Sato (1994) theory

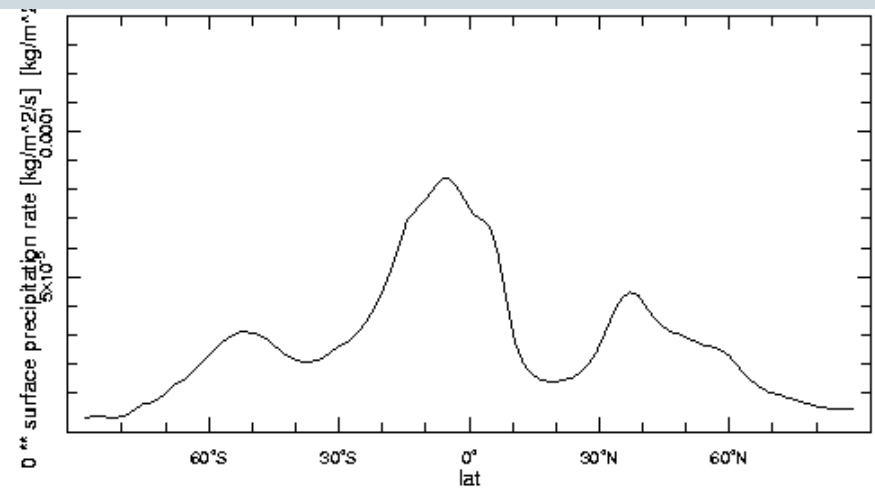


- Seasonal precip (July mean and December mean)



Jul

July precip



Jan

December precip

- We'll discuss models with active moisture shortly
 - These predict the width of the precipitating regions as well

Next: effect of eddies on the Hadley circulation



- We talked about ways to incorporate eddy heat fluxes into an axisymmetric model
- How about effect of eddy momentum fluxes?
 - Ferrel cell derivation
 - An eddy-driven Hadley cell model

Effect of eddy fluxes

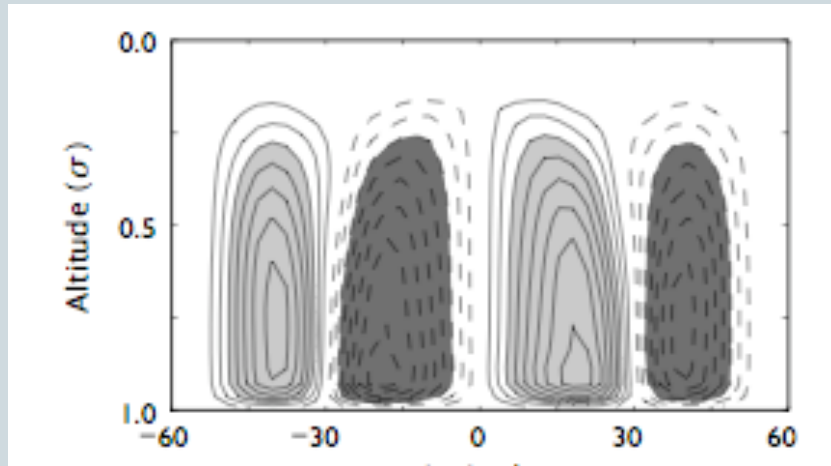


- Compare the dry dynamical core model run axisymmetrically versus with eddies
 - Hadley cell is significantly stronger with eddies
 - Suggests eddies are a major driver in this model!
 - Heat fluxes or momentum fluxes?
- Not true in moist model!
 - Axisymmetric cell is stronger in moist GCM
 - Comparing axisymmetric and full Hadley cells in different models could be nice project

Dry GCM Results

- Hadley cell strengths:

Model



Obs

